

**Theory of Computation, CSCI 438 spring 2022**  
**Undecidability, 201-202, April 8**

Recall:

$A_{DFA} = \{ \langle D, w \rangle \mid D \text{ is a DFA, } w \text{ is a string in the language of } D, \text{ and } w \in \mathcal{L}(D) \}$  is decidable. (Acceptance problem for DFAs)

$A_{NFA} = \{ \langle D, w \rangle \mid D \text{ is an NFA, } w \text{ is a string in the language of NFA and } w \in \mathcal{L}(D) \}$  is decidable. (Acceptance problem for NFAs)

$A_{CFG} = \{ \langle G, w \rangle \mid G \text{ is a CFG, } w \text{ is a string in the language of } G, \text{ and } w \in \mathcal{L}(G) \}$  is decidable. (Acceptance problem for CFG)

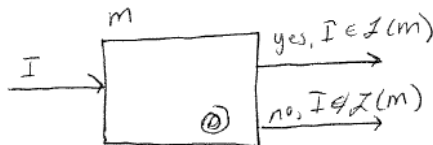
How about:  $A_{Reg}$ ,  $A_{PDA}$ ?

Can draw machines as boxes, showing the inputs and outputs.

Example, any decider:



Example, any recognizer:



Example, decider for an acceptance problem for some class of machines:



Is  $A_{TM} = \{ \langle M, w \rangle \mid M \text{ is a TM, } w \text{ is a string in the alphabet of the TM and } w \in \mathcal{L}(M) \}$  decidable? (I.e. is the acceptance problem for TM decidable?)

Can draw machines as boxes, showing the inputs and outputs.