

**Theory of Computation, CSCI 438 spring 2022**  
**Context-free grammars, pages 101-107, Feb. 9**

1. Give a context free grammar for the language on  $\Sigma=\{a,b\}$  defined by  
 $L=\{w \mid w=w^R \text{ for } w \in \Sigma^*, \text{ that is, } w \text{ is a palindrome}\}$
2. Give a context free grammar for the language on  $\Sigma=\{a,b\}$  defined by  
 $L=\{a^n b^n : n \geq 0\}$
3. Give a context free grammar for the language on  $\Sigma=\{0,1\}$  defined by  
 $L= \{w \mid w \text{ starts and ends with the same symbol}\}$
4. Give a context free grammar for the language on  $\Sigma=\{0,1\}$  defined by  
 $L= \{w \mid w \text{ contains at least three } 1\text{'s}\}$

5. Define a context-free grammar for the following language  
 $L = \{w \mid (n_a(w) - n_b(w)) \bmod 3 = 1\}$

6. Create a context-free grammar for the language  
 $L = \{w\#x \mid w^R \text{ is a substring of } x \text{ for } w, x \in \{0,1\}^*\}$   
(This is exercise 2.6c in the text.)

7. Give a context free grammar for the language on  $\Sigma = \{a,b\}$  defined by  
 $L = \{w \mid (n_a(w) > n_b(w))\}$ .  
The set of strings over the alphabet  $\{a,b\}$  with more a's than b's  
 $n_a(w)$  is the number of a's in the string  $w$ .  
 $n_b(w)$  is the number of b's in the string  $w$ .