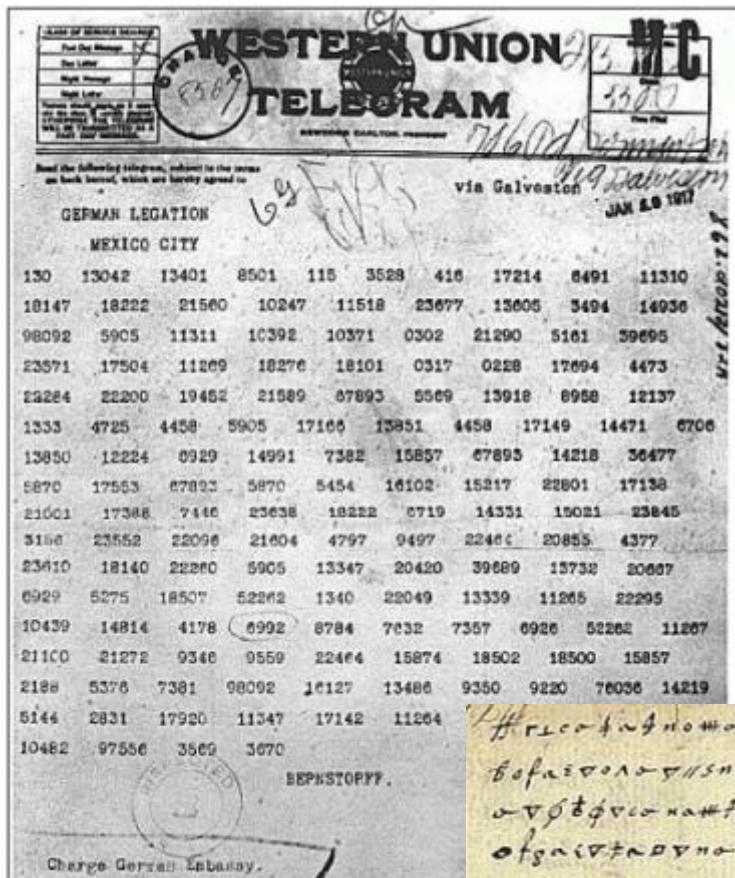


# Historical cryptography



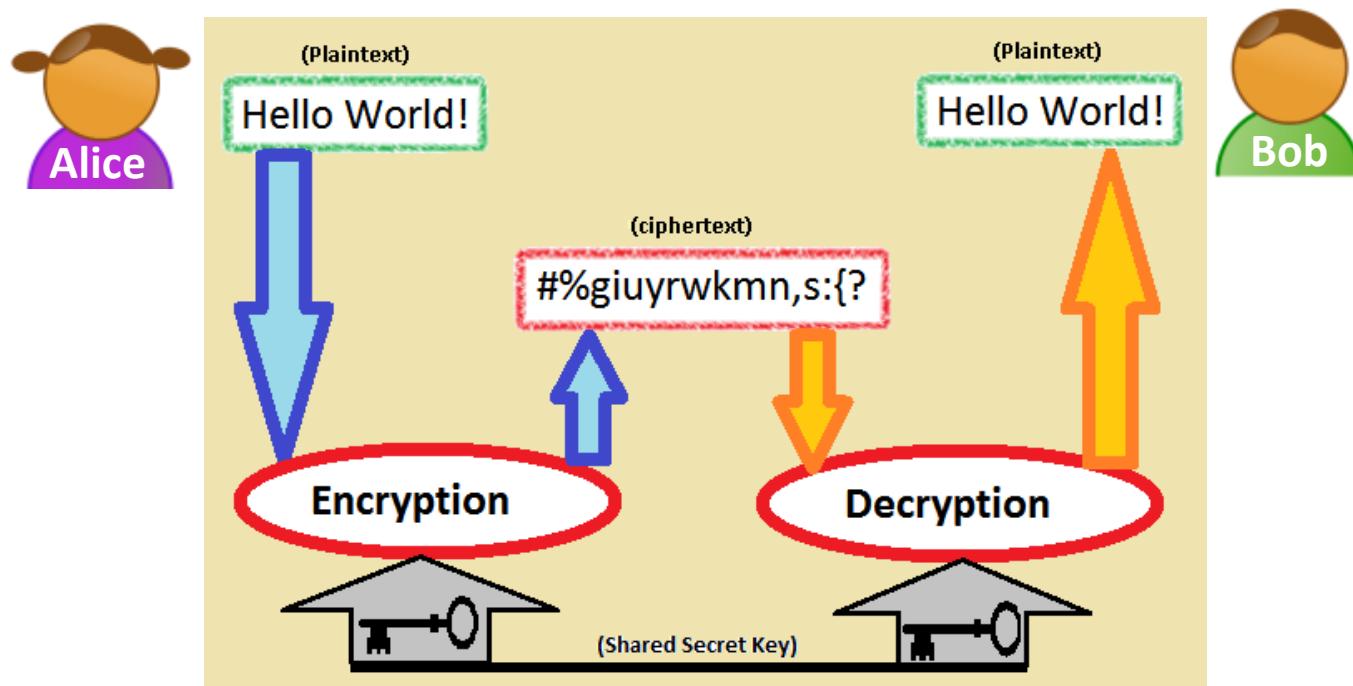
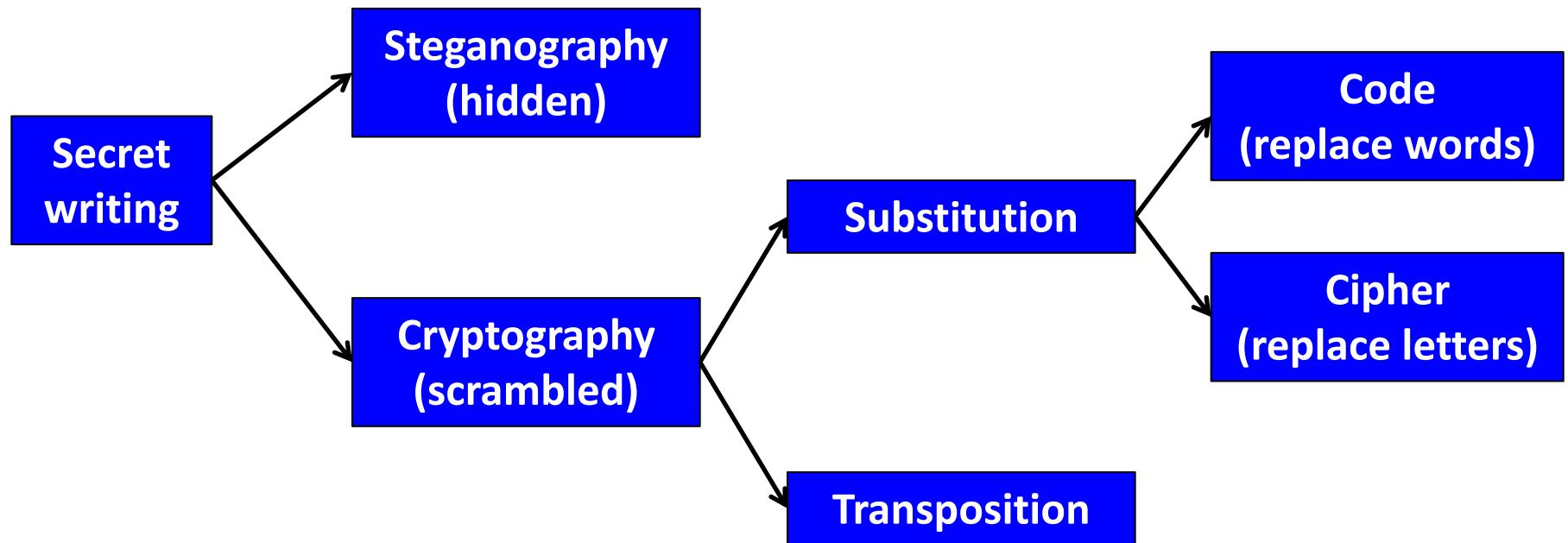
Bundesarchiv, Bild 101I-241-2172-06  
Foto: Gruppe I 1437/044

17149 14471 6706  
15217 22801 17138  
14331 15021 23845  
22484 20855 4377  
39689 15732 20667  
13339 11265 22295  
7632 7357 6926  
18502 18500 15857  
13486 9350 9220  
76036 14219

17149 14471 6706  
15217 22801 17138  
14331 15021 23845  
22484 20855 4377  
39689 15732 20667  
13339 11265 22295  
7632 7357 6926  
18502 18500 15857  
13486 9350 9220  
76036 14219

# Overview

- Historical cryptography
  - Monoalphabetic substitution ciphers
    - Breaking them
    - Some improvements
    - The cipher of Mary Queen of Scots
  - Polyalphabetic substitution ciphers
  - Unbreakable encryption
  - WWI
    - Zimmerman telegram
  - WWII
    - Rise of the cipher machines
    - Enigma



# Monoalphabetic ciphers

- Monoalphabetic cipher
  - Use a fixed substitution over entire message
- Assigning substitutions
  - Option 1: Caesar shift cipher
  - Option 2: Completely random
    - $26!$  ways to assign  $\approx$  400,000,000,000,000,000,000
    - But hard to remember a completely random assignment
  - Option 3: Based on key phrase
    - Shared secret: "ugly black swan"

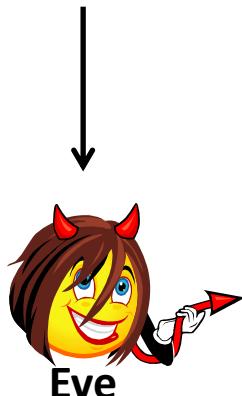
a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
U	G	L	Y	B	A	C	K	S	W	N	D	E	F	H	I	J	M	O	P	Q	R	T	V	X	Z



# Breaking a monoalphabetic cipher



LIVITCSWPIYVEWHEVSRIQMXXLEYVEOIEWHRXEXIPFEMVEWHKVSTYLXZIXLIKIIIX  
PIJVSZEYPERRGERIMWQLMGLMXQERIWGPSRIHMXQEREKIETXMJTPRGEVEKEITRE  
WHEXXLEXXMZITWAWSQWXSWEXTVEPMRXRSJGSTVRIEYVIEXCVMUIMWERGMIWXMJ  
MGCSMWXSJOMIQXLIVIQIVIXQSVSTWHKPEGARCSXRWIEVSWIIBXVIIZMXFSJXLIK  
EGAEWHEPSWYSWIWIEVXLISXLIVXLIRGEPIRQIVIIBGIIHMWYPFLEVHEWHYPSSRR  
FQMXLEPPXLIECCIEVEWGJSJKTVWMRLIHYSPHXLIQIMYLXSJXLIMWRIGXQEROIV  
FVIIZEVAEKPIEWHXEAMWYEPPXLMWYRMWXSGSWRMHIVEXMSWMGSTPHLEVHPFKPEZ  
INTCMXIVJSVLMRSCMWMSSWVIRCIGXMWYMX

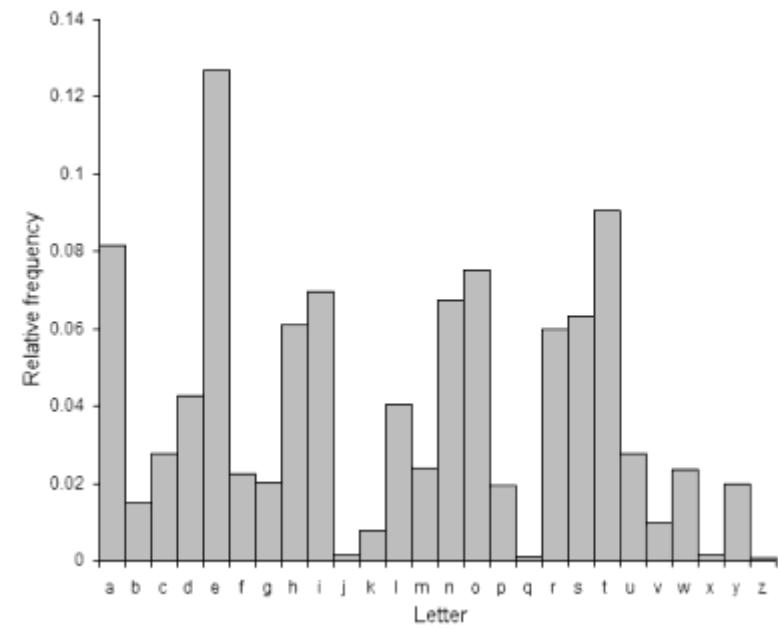


Eve counts up frequency of  
single letters, letter pairs  
(bigrams), letter triples  
(trigrams)

# Breaking a monoalphabetic cipher: step 1

LIVITCSWPIYVEWHEVSRIQMXLEYVEOIEWHRXEXIPFEMVEHKVSTYLXZIXLIKIIIX  
PIJVSZEYPERRGERIMWQLMGLMXQERIWGSPRIHMXQEREKIETXMJTPRGEVEKEITRE  
WHEXXLEXXMZITWAWSQWXSWEXTVEPMRXRSJGSTVRIEYVIEXCVMUIMWERGMIWXMJ  
MGCSMWXSJOMIQXLIVIQIVIXQSVSTWHKPEGARCSXRWIEVSWIIBXVIZMXFSJXLIK  
EGAEWHEPSWYSWIWIEVXLISXLIVXLIRGEPIRQIVIIBGIIHMWYPFLEVHEWHYPSSRR  
FQMXLEPPXLIECCIEVEWGJSKTVWMRLIHYSPHXLIQIMYLXSJXLIMWRIGXQEROIV  
FVIIZEVAEKPIEWHXEAMWYEPPXLMWYRMWXSGSWRMHIVEXMSWMGSTPHLEVHPFKPEZ  
INTCMXIVJSVLMRSCMWMSSWVIRCIGXMWYMX

ciphertext	plaintext	
I	e	most common letter
XL	th	most common bigram
XLI	the	most common trigram
E	a	second most common letter

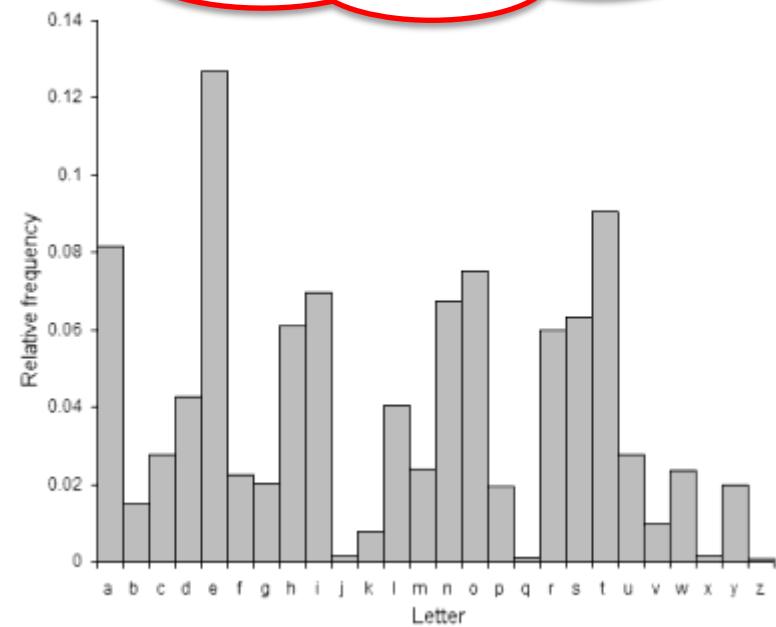


# Breaking a monoalphabetic cipher: step 1

heVeTCSWPeYVaWHaVSReQMthaYVaOeaWHRtatePFaMVaWHKVSTYhtZetheKeet  
PeJVSZaYPaRRGaReMWQhMGhMtQaReWGPsReHMTQaRaKeaTtMJTPRGaVaKaeTRA  
WHatthattMZeTWAWSQWtSWatTVaPMRtRSJGSTVReaYVeatCVMUeMWaRGMeWtMJ  
MGCSMWTsJOMeQtheVeQeVetQSVSTWHKPAGARCStRWeaVSWeeBtVeZMtFSJtheK  
aGAaWHaPSWYSWeWeaVtheStheVtheRGaPeRQeVeeBGeemHWYPFhaVHaWHYPSRR  
FQMthaPPtheaCCeaVaWGeSJKTWVWRheHYSPHtheQeMYhtSJtheMWReGtQaROeV  
FVeZaVAaKPeaWhtaAMWYaPPthMWYRMWtSGSWRMHeVatMSWMGSTPHaVHPFKPaZ  
eNTCMteVJSVhMRSCMWMWSVeRCeGtMWYMT

Eve now has a partially decoded message.

ciphertext	plaintext	
I	e	most common letter
XL	th	most common bigram
XLI	the	most common trigram
E	a	second most common letter



# Breaking a monoalphabetic cipher: step 2

heVeTCSWPeYVaWHaVSReQMthaYVaOeaWH**Rtate**PFaMVaWHKVSTYhtZetheKeet  
PeJVSZaYPaRRGaReMWQhMGhMtQaReWGPsReHMTQaRaKeaTtMJTPRGaVaKaeTRA  
**WhatthattMZe**TWAWSQWtSWatTVaPMRtRSJGSTVReaYVeatCVMUeMWaRGMeWtMJ  
MGCSMWTsJOMeQtheVeQeVetQSVSTWHKPAGARCStRWeaVSWeeBtVeZMtFSJtheK  
aGAaWHApsWYSWeWeavtheStheVtheRGaPeRQeVeeBGeEHMWYPFhaVHaWHYPSRR  
FQMthaPPtheaCCeaVaWGeSJKTvWMRheHYSPHtheQeMYhtSJtheMWReGtQaROeV  
FVeZaVAakPeaWhtaAMWYaPPthMWYRMWtSGSWRMHeVatMSWMGSTPHaVHPFKPaZ  
eNTCMteVJSVhMRSCMWMSSWVeRCeGtMWYMT

ciphertext	plaintext	cipher fragment	plaintext guess
V	r	heVe	here
R	s	Rtate	state
M	i	atthattMZe	atthattime
Z	m	atthattMZe	atthattime



Eve can now use language knowledge to make further guesses...

# Breaking a monoalphabetic cipher

```
hereTCSWPeYraWHarSseQithaYraOeaWHstatePFairaWHKrSTYhtmetheKeet  
PeJrSmaYPassGaseiWQhiGhitQaseWGPSsseHitQasaKeaTtiJTPsGaraKaeTsa  
WHatthattimeTWAWSQWtSWatTraPistssJGSTrseaYreatCriUeiWasGieWtiJ  
iGCSiWtSJQieQthereQeretQSrSTWHKPaGAsCStsWearSWeeBtremitFSJtheK  
aGAaWHaPSWYSWeWeartheStherthesGaPesQereeBGeeshiWYPFharHaWHYPSss  
FQithaPPtheaCCearaWGeSJKTrWisheHYSPHtheQeiYhtSJtheiwseGtQasOer  
FremarAaKPearWHtaAiWYaPPthiWYsiWtSGSWsiHeratiSWiGSTPHarHPFKPam  
eNTCiterJSrhisSCIWiSWresCeGtiWYit
```

and so on...



# Decoded monoalphabetic cipher

hereupon legrand arose with a grave and stately air and brought me the beetle from a glass case in which it was enclosed. It was a beautiful scarabaeus, and, at that time, unknown to naturalists—of course a great prize in a scientific point of view. There were two round black spots near one extremity of the back, and a long one near the other. The scales were exceedingly hard and glossy, with all the appearance of burnished gold. The weight of the insect was very remarkable, and, taking all things into consideration, I could hardly blame Jupiter for his opinion respecting it.

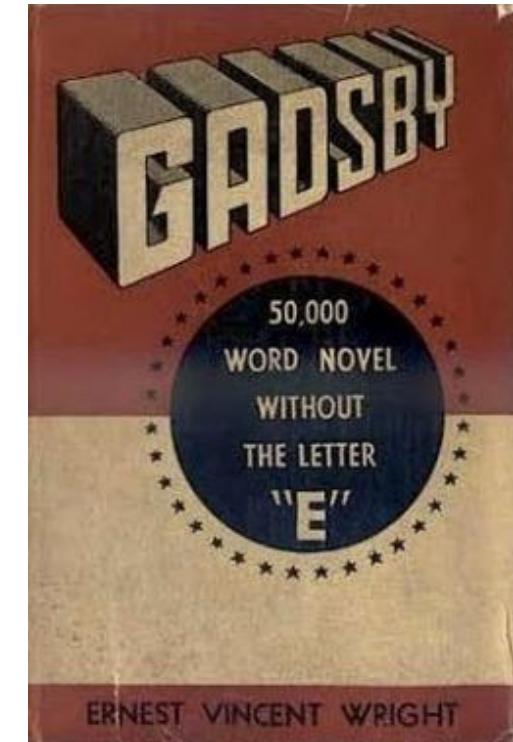
Hereupon Legrand arose, with a grave and stately air, and brought me the beetle from a glass case in which it was enclosed. It was a beautiful scarabaeus, and, at that time, unknown to naturalists—of course a great prize in a scientific point of view. There were two round black spots near one extremity of the back, and a long one near the other. The scales were exceedingly hard and glossy, with all the appearance of burnished gold. The weight of the insect was very remarkable, and, taking all things into consideration, I could hardly blame Jupiter for his opinion respecting it.

# Or use some code from the Internet...

```
c:\Dropbox\mtech\websci\resources>simpsub2.exe
Name of sample ("learning") file: moby.txt
Name of cipher file: mono2.txt
Is the cipher formatted with spaces? (y/n): n
Reading sample file...
Analyzing sample file...
Reading cipher file...
Analyzing cipher file...
Initial closeness is 1.487429, PLEASE WAIT...
DONE! Func value=0.866612
Key is: abcdefghijklmnopqrstuvwxyz
          ekghijylmdapzwscnvrxtqbfu
hereuponlegrandarosewithagraveandstatelyairandbroughtmethebeetlefromaglasscaseinwhichitwasencloseditwasabeautifulscaraeusandalthattimeunknowntonaturalistsofcourseagreatprizeinascientificpointofviewthereweretwroundblackspotsnearoneextremityofthebackandalongoneneartheotherthescaleswereexceedinglyhardandglossywithalltheappearanceofburnishedgoldtheweighthoftheinsectwasveryremarkableandtakingallthingsintoconsiderationicouldhardlyblamequpiterforhisopinionrespectingit
```

# Shoring up monoalphabetic ciphers

- Improved resistance to frequency analysis:
  - Insert nulls, symbols that represent nothing
    - e.g. cipher alphabet 1-99, 73 numbers represent nulls
  - Mespall thangs on pirpus
    - Screws up frequency, humans can correct
  - Use code words
    - Need to exchange large dictionary of codes
    - Capture of codebook destroys security
  - Homophonic substitution
    - Multiple cipher symbols per plaintext symbol
  - Nomenclature
    - Small list of words/syllables
    - Cipher alphabet with homophones



# Homophonic substitution

- Improved resistance to frequency analysis:
  - Homophonic substitution
    - Plaintext symbol, set of cipher symbols
    - Set size proportional to frequency in the language

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
09	48	13	01	14	10	06	23	32	15	04	26	22	18	00	38	94	29	11	17	08	34	60	28	21	02
12	81	41	03	16	31	25	39	70			37	27	58	05	95		35	19	20	61		89		52	
33		62	45	24		50	73			51		59	07			40	36	30	63						
47			79	44		56	83			84		66	54			42	76	43							
53				46		65	88					71	72			77	86	49							
67					55		68	93				91	90			80	96	69							
78						57						99						75							
92							64											85							
							74											97							
							82																		
							87																		
							98																		

# Mary Queen of Scots

- **Babington Plot**

- Mary imprisoned for 18 years
- Gilbert Gifford double agent "recruited" to communicate with Mary
- Detoured letters via Walsingham
- Anthony Babington and company
  - Rescue Mary
  - Assassinate Elizabeth
  - Wanted blessing of Mary



*Mary Queen of Scots*



*Elizabeth I*



*Francis Walsingham*

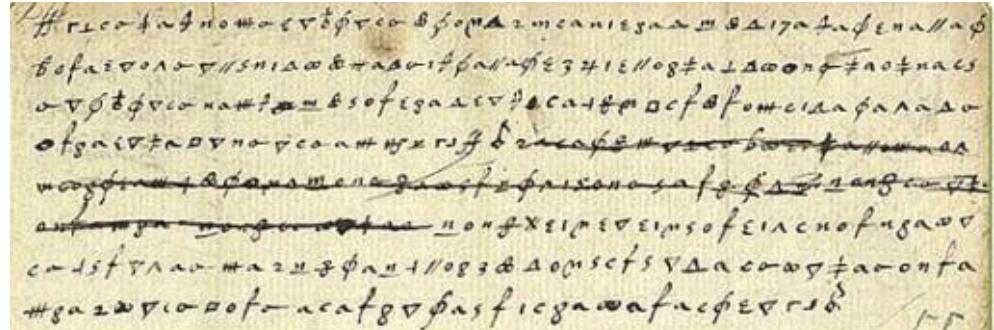


# The plot

- Babington plot
  - Gifford delivers message from Mary to Babington
  - Babington replies with outline of plot

"Myself with ten gentlemen and a hundred of our followers will undertake the delivery of your royal person from the hands of your enemies. For the dispatch of the usurper, from the obedience of whom we are by the excommunication of her made free, there be six noble gentlemen, all my private friends, who for the zeal they bear to the Catholic cause and your Majesty's service will undertake that tragical execution"

- Mary replies endorsing plan
- Walsingham forges postscript to Mary's letter asking Babington to name names





Den viii february werde onthalst Maria

Shaeck Schot v Comynne s tevende sconck Calpe-  
sych hebbende gesoest vcc ontust ten den te riechten haer schot  
met her te grachten van Engeland t doedesch haer vrouwe sconck  
ofte parlement regemintelyk voerde verloent. Anno 1585.

Martini xiii sol xiiii m xiii v

# Polyalphabetic cipher

- Monoalphabetic cipher
  - Single set of substitutions for all letters

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
U	G	L	Y	B	A	C	K	S	W	N	D	E	F	H	I	J	M	O	P	Q	R	T	V	X	Z

- Polyalphabetic cipher
  - Multiple sets of substitutions
  - Switch between them during encryption
  - 1460s, Leon Alberti hits on idea of using 2+ sets

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
U	G	L	Y	B	A	C	K	S	W	N	D	E	F	H	I	J	M	O	P	Q	R	T	V	X	Z
T	H	E	Q	U	I	C	K	B	R	O	W	N	F	X	J	M	P	S	V	L	A	Z	Y	D	G

# Polyalphabetic cipher

- 1586, Vigenère cipher
  - "Le Chiffre Indéchiffrable"
  - Letters Caesar shifted, change based on keyword

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	
A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	
B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	
C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	
D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	
F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	
G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	
I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	
L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	
M	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y



*Blaise de Vigenère*

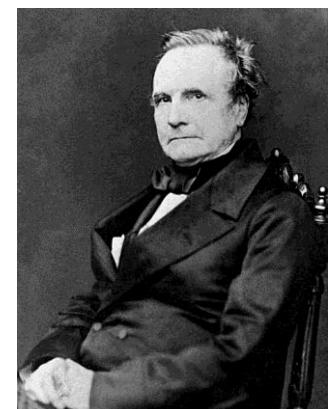
Plaintext	attackatdawn
Key	LEMONLEMONLE
Ciphertext	LXFOPVEFRNHR

# Breaking the Vigenère Cipher

- **Vigenère cipher**
  - Much better at hiding letter frequency info
  - But key repeats:
    - If you know length, an interwoven set of Caesar ciphers

<b>Key :</b>	ABCDABCDABCDABCDABCDABCDABCD
<b>Plaintext:</b>	CRYPTO IS SHORT FOR CRYPTOGRAPHY
<b>Ciphertext:</b>	CSASTPKVSIQUTGQU CSASTPIUAQJB

- Distance between repeats = 16
- Suggests key length if 16, 8, 4, 2, or 1
- Find additional repeats to narrow lengths
- Frequency analyze each interwoven set



*Charles Babbage*

# WWI: Zimmermann Telegram

- 1915, U-boat sinks Lusitania
  - 128 US Civilians killed
  - Germany promises to surface first
- 1916, new Foreign Minister
  - Arthur Zimmermann
- 1917, unrestricted submarine warfare
  - Zimmermann hatches plan
    - Keep American busy at home
    - Persuade Mexico to invade US and invite Japan to attack as well



*Arthur Zimmermann*

CLASS OF SERVICE DELIVERY	
Five Day Message	
One Line	
Night Message	
Night Letter	
Please initial here if you want your telegram sent by AIR MAIL. An additional charge will be transmitted as a FEE FOR AIR MESSAGE.	



NEW YORK, CARLTON, PRENTISS

Send the following telegram, subject to the terms  
as back letter, which are hereby agreed to:

GERMAN LEGATION

MEXICO CITY

130 13042 13401 8501 115 3528 416 17214 8491 11310  
 18147 18222 21560 10247 11518 23677 13605 3494 14936  
 98092 5905 11311 10392 10371 0302 21290 5161 59695  
 23571 17504 11269 18276 18101 0317 0228 17694 4473  
 23284 22200 19452 21589 67893 5569 13918 8958 12137  
 1333 4725 4458 5905 17166 13851 4458 17149 14471 6706  
 13850 12224 6929 14991 7382 15857 67893 14218 36477  
 5870 17553 67893 5870 5454 16102 15217 22801 17138  
 21001 17388 7440 23638 18222 0719 14331 15021 23845  
 3156 23552 22096 21604 4797 9497 22464 20855 4377  
 23610 18140 22260 5905 13347 20420 39689 13732 20667  
 0929 5275 18507 52262 1340 22049 13339 11265 22295  
 10439 14814 4178 6992 8784 7632 7357 6926 52262 11267  
 21100 21272 9348 9559 22464 15874 18502 18500 15857  
 2186 5376 7381 98092 16127 13486 9350 9220 76036 14219  
 5144 2831 17920 11347 17142 11264 7667 7762 15099 9110  
 10482 97556 3569 3670

REPNSTOPFF.

Charge German Embassy.

MC

53007

Two P.M.

RECEIVED  
1-8-58  
U.S. State Dept.

## TELEGRAM RECEIVED.

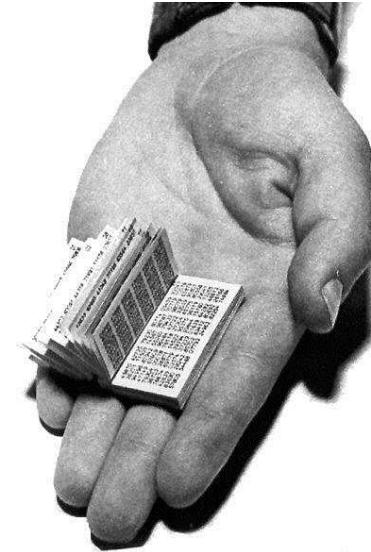
FROM 2nd from London # 5747.

By Winfred E. Hoffmeyer  
Date Oct 22, 1914

"We intend to begin on the first of February unrestricted submarine warfare. We shall endeavor in spite of this to keep the United States of America neutral. In the event of this not succeeding, we make Mexico a proposal of alliance on the following basis: make war together, make peace together, generous financial support and an understanding on our part that Mexico is to reconquer the lost territory in Texas, New Mexico, and Arizona. The settlement in detail is left to you. You will inform the President of the above most secretly as soon as the outbreak of war with the United States of America is certain and add the suggestion that he should, on his own initiative, ~~invite~~ Japan to immediate adherence and at the same time mediate between Japan and ourselves. Please call the President's attention to the fact that the ruthless employment of our submarines now offers the prospect of compelling England in a few months to make peace." Signed, ZIMMERMANN.

# Unbreakable encryption

- 1882, One-time pad
  - Use a key as long as the message
  - Choose the key (truly) randomly
  - Only use the key once and only once
  - Provably secure



H	E	L	L	O	message
7 (H)	4 (E)	11 (L)	11 (L)	14 (O)	message
+ 23 (X)	12 (M)	2 (C)	10 (K)	11 (L)	key
= 30	16	13	21	25	message + key
= 4 (E)	16 (Q)	13 (N)	21 (V)	25 (Z)	message + key (mod 26)
E	Q	N	V	Z	ciphertext

E	Q	N	V	Z	ciphertext
4 (E)	16 (Q)	13 (N)	21 (V)	25 (Z)	ciphertext
- 23 (X)	12 (M)	2 (C)	10 (K)	11 (L)	key
= -19	4	11	11	14	ciphertext - key
= 7 (H)	4 (E)	11 (L)	11 (L)	14 (O)	ciphertext - key (mod 26)
H	E	L	L	O	message

# Breaking one-time pads?

- Try all possible keys
  - $26^{\text{length}}$  = big
  - Generates all possible sequences

E	Q	N	V	Z	ciphertext
4 (E)	16 (Q)	13 (N)	21 (V)	25 (Z)	ciphertext
- 23 (X)	12 (M)	2 (C)	10 (K)	11 (L)	key
= -19	4	11	11	14	ciphertext - key
= 7 (H)	4 (E)	11 (L)	11 (L)	14 (O)	ciphertext - key (mod 26)
H	E	L	L	0	message

Correct  
key

E	Q	N	V	Z	ciphertext
4 (E)	16 (Q)	13 (N)	21 (V)	25 (Z)	ciphertext
- 19 (T)	16 (Q)	20 (U)	17 (R)	8 (I)	possible key
= -15	0	-7	4	17	ciphertext-key
= 11 (L)	0 (A)	19 (T)	4 (E)	17 (R)	ciphertext-key (mod 26)
L	A	T	E	R	possible message

Some  
other key

# Unbreakable encryption

- Problems with one-time pads:
  - Must distribute pads securely
  - Must use truly random numbers
    - Not pseudo-random
    - Not random typing on a keyboard
  - Must never reuse the same key

ДЛЯ РАСПРОСТРАНЕНИЯ	95	1100
24765 93659 55146	09380	18862 67698 69598
25341 88038 31282	36957	21708 51305 66499
65096 02819 74377	27960	20471 53361 18687
19226 31329 55134	83869	26588 24850 81322
01334 80225 37061	13995	88627 07293 53021
98865 91712 80927	18799	71311 57151 71976
98890 61224 59636	08076	65747 36834 49525
95428 50476 06584	38300	37155 75549 11968
43041 83175 29737	88523	76769 29465 47144
77230 19601 57378	51440	48830 63857 15846
32548 48508 71999	22399	86499 23635 91365
57311 83798 06280	74855	58916 46616 07784
10464 00582 08702	30607	80017 50120 76361
93610 38382 57828	27710	00947 00977 02927
53217 20255 20839	63759	74008 50213 32159
31617 14857 97505	25301	14258 36792 42161
52190 32626 07392	88180	32382 22884 82072
39585 92345 44974	09467	88114 50578 84634
44347 73224 49702	60171	56691 11969 32188
06468 37447 02998	93679	05391 95625 21874
85784 28585 57163	61054	85038 41729 76885
12105 61287 69331	72620	98079 56863 59622
94389 88086 36174	39492	54706 56234 49308
79987 13807 72453	07594	89880 63808 18102
65413 91747 01977	31100	62600 78129 31020
09685 11575 35283	37365	15236 28014 82731
35772 51501 01308	09111	40637 41959 81825
69421 13874 28982	52087	95908 43908 26669
64308 31080 08437	64768	79907 58033 78288
39151 32450 44942	53264	04459 19196 33063
57000 78066 10301	31438	87160 08879 10617
41192 47297 79960	45748	24756 60210 83200
91761 48988 10844	64704	86812 61530 69324
03174 79631 96669	88017	31989 32177 73058
94449 59824 50666	22217	36665 78788 88951
92675 67684 01497	28710	65502 37546 76036
84157 68553 92307	42962	21660 78980 52154
57646 07563 92053	84974	34262 59764 68318
65986 82656 13413	64402	77821 46520 50332
43525 90572 90036	01483	75550 94795 48699

"As a practical person, I've observed that one-time pads are theoretically unbreakable, but practically very weak. By contrast, conventional ciphers are theoretically breakable, but practically strong."

-Steve Bellovin

# Mechanization of secret writing

- Pencil and paper
  - Security limited by what humans can do quickly and accurately in the heat of battle
- Enter the machine



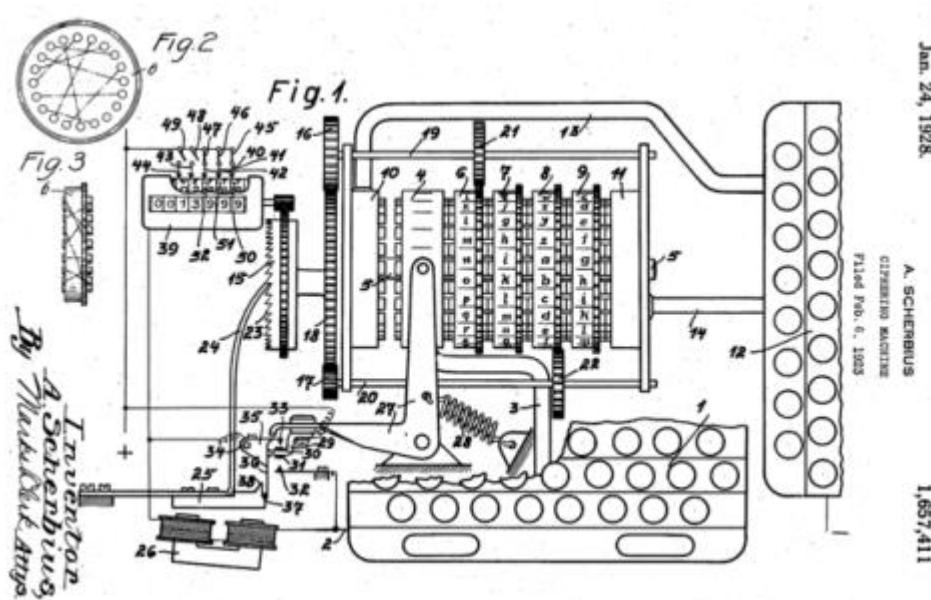
*Thomas Jefferson's wheel cipher*



*Captain Midnight's Code-o-Graph*

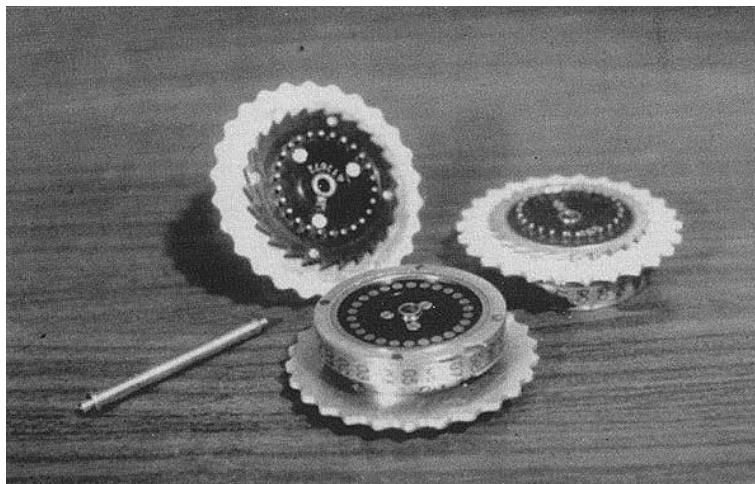
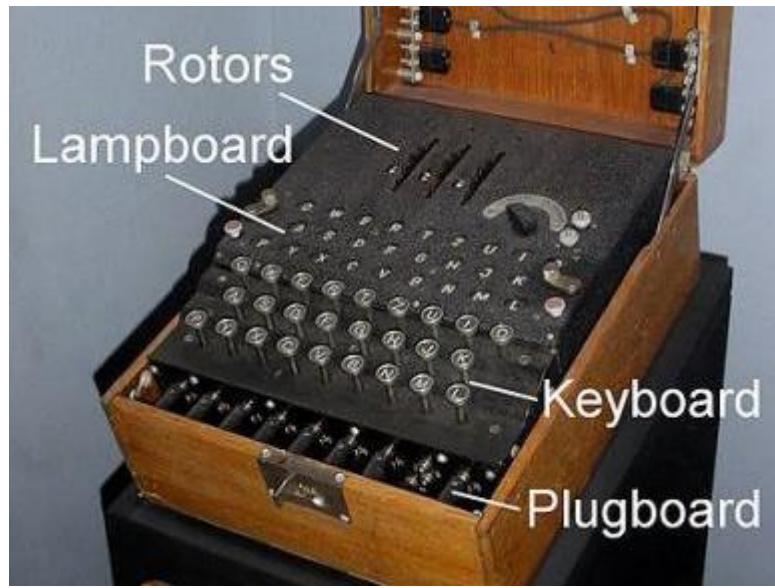
# Enigma machine

- Enigma cipher machine
  - 1918, patented by German engineer Arthur Scherbius



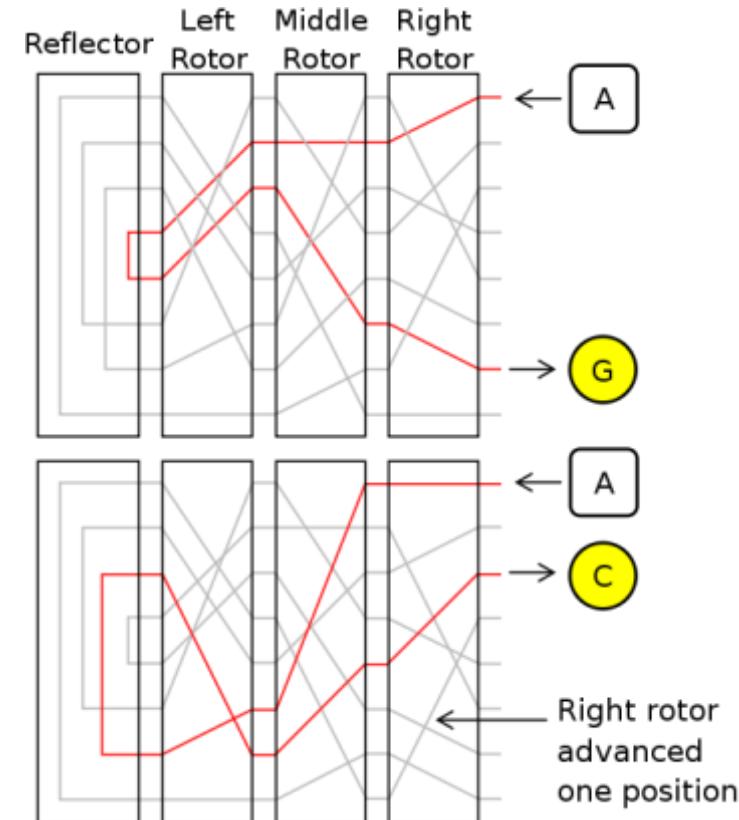
Arthur Scherbius

- A electrical/mechanical implementation of a polyalphabetic substitution cipher



# Enigma rotors

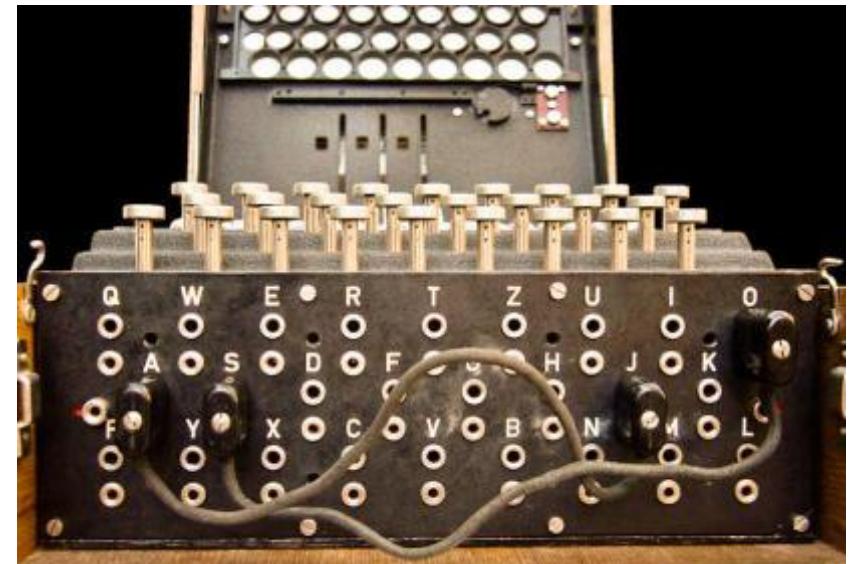
- Rotor (wheel, drum)
  - An monoalphabetic substitution cipher implemented via a complex wiring pattern
  - Set to one of 26 initial positions
  - Geared to rotate after each letter
- Rotor set
  - 3 rotors in  $3! = 6$  possible orders
    - Eventually set increased to 3 out of 5
    - Navy used even more
  - Possible keys:
    - $3! * 26^3 = 6 * 17,576 = 105,456$



# Enigma plugboard

- **Plugboard**

- Operate inserts cables to swap letters
- Initially 6 cables
  - Swaps 6 pairs of letters
  - Leaves 14 letters unswapped
- Possible configurations:
  - 100,391,791,500



- **Total keys:**

- $17,576 * 6 * 100,391,791,500 \approx 10,000,000,000,000,000$

# Enigma

- **Enigma machine**

- Sales initially slow
- 1923, Germans find out about failures of communication security in WWI
- 1925, Scherbius starts mass production
- German military eventually buys 30,000 Enigma machines
- 1929, Scherbius dies in carriage accident



Photo: BSA 03-000-075-022  
Foto: Walter J. Röhr / Imagno



*Arthur Scherbius*

# Cracking the Enigma

- Step 1: Espionage

- Disgruntled Schmidt meets with French secret agent
- Sells Enigma user manuals
  - Allows replica to be constructed
  - Also codebook and daily key scheme
- French just give intelligence to Poles



"It is assumed in judging the security of the cryptosystem that the enemy has at his disposition the machine."

-German memorandum

*Hans-Thilo Schmidt*

# Cracking the Enigma

- Step 2: Poles identify weakness

- German's had day code specifying:

- Configuration of rotors
    - Settings of rotors
    - Settings of plugboard

- Unique key per message:

- Send 3 letters, encrypted with day key
    - Letters specify new setting of rotors
    - New rotors setting used for message payload
    - Repeat the 3 initial letters twice



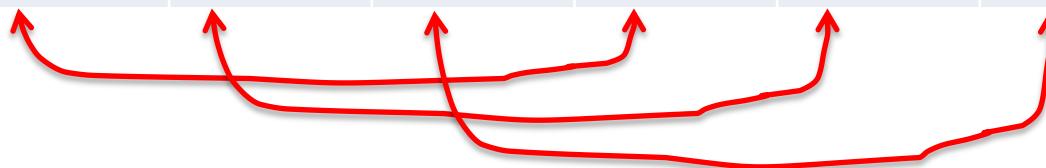
*Marian Rejewski*

**Repetition is the enemy of security!**

# Cracking the Enigma

- Find patterns in first 6 letters
  - 1<sup>st</sup>-4<sup>th</sup>, 2<sup>nd</sup>-5<sup>th</sup>, 3<sup>rd</sup>-6<sup>th</sup> are ciphers of same letter

Message	1st	2nd	3rd	4th	5th	6th
1	L	O	K	R	G	M
2	M	V	T	X	Z	E
3	J	K	T	M	P	E
4	D	V	Y	P	Z	X

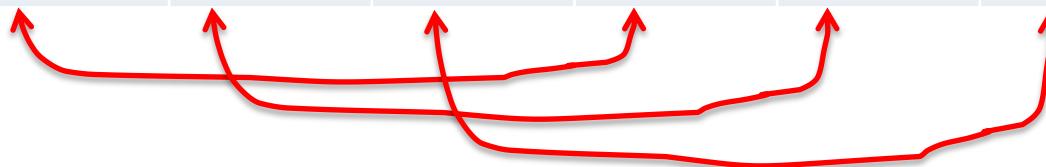


1 <sup>st</sup>	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
4 <sup>th</sup>				P						M	R	X														

# Cracking the Enigma

- Given enough messages:
  - Fill in full table of relations between 3 pairs

Message	1st	2nd	3rd	4th	5th	6th
1	L	O	K	R	G	M
2	M	V	T	X	Z	E
3	J	K	T	M	P	E
4	D	V	Y	P	Z	X



1 <sup>st</sup>	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
4 <sup>th</sup>	F	Q	H	P	L	W	O	G	B	M	V	R	X	U	Y	C	Z	I	T	N	J	E	A	S	D	K

# Fingerprinting a day key

- Find chains
  - Chains change each day depending on day key

1 <sup>st</sup>	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
4 <sup>th</sup>	F	Q	H	P	L	W	O	G	B	M	V	R	X	U	Y	C	Z	I	T	N	J	E	A	S	D	K

A → F → W → A	3 links
B → Q → Z → K → V → E → L → R → I → B	9 links
C → H → G → O → Y → D → P → C	7 links
J → M → X → S → T → N → U → J	7 links

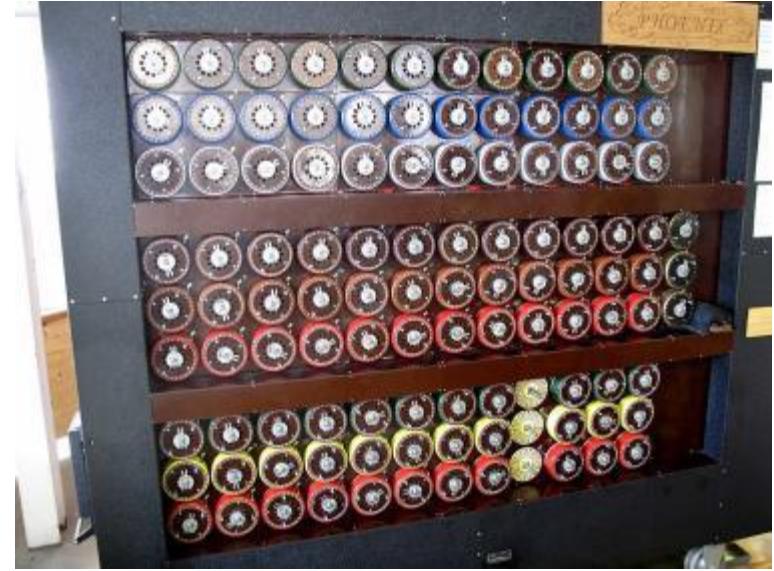
- Also for 2<sup>nd</sup>-5<sup>th</sup> and 3<sup>rd</sup>-6<sup>th</sup> letter pairs
- # of chains and length, independent of plugboard
- Catalog 105,456 rotors settings using replica

# WWII

- 1938, Germany increases Enigma security
  - Add two additional rotors,  $C(5, 3) = 60$
  - 10 plugboard cables instead of 6
  - Poles couldn't build big enough "bombe"
  - Poles hand over research to British/French



*US Navy bombe*



*Bletchley Park bombe*

# Bletchley Park

- **Government Code and Cypher School**
  - Height of WWII, 9000 people
  - Battled against improvements to Enigma
  - May 1, 1940 Germans stop repetition of msg key
    - Turing had already developed technique + machine to crack using "crib" instead of repetition of key



*Alan Turing*



# Cribs

- Cribs
  - Some plaintext you think is in the ciphertext
    - Ideally also the location
    - e.g. Germans usually broadcast weather at 6am
      - "wetter" somewhere at start of message
  - German Navy had strongest crypto:
    - 3 rotors out of 8, reflector with 26 orientations
    - Avoided stereotypical messages
  - Allies:
    - Mine area to generate traffic
      - Grid reference as crib
    - Also, stole code books



Type VII U-boot

# Summary

- History of Cryptography
  - Substitution ciphers
    - Monoalphabetic
    - Polyalphabetic
  - One-time pads
    - Provably unbreakable
      - (if used carefully)
  - Cryptography in WWI and WWII
    - Zimmerman telegraph
    - Enigma

