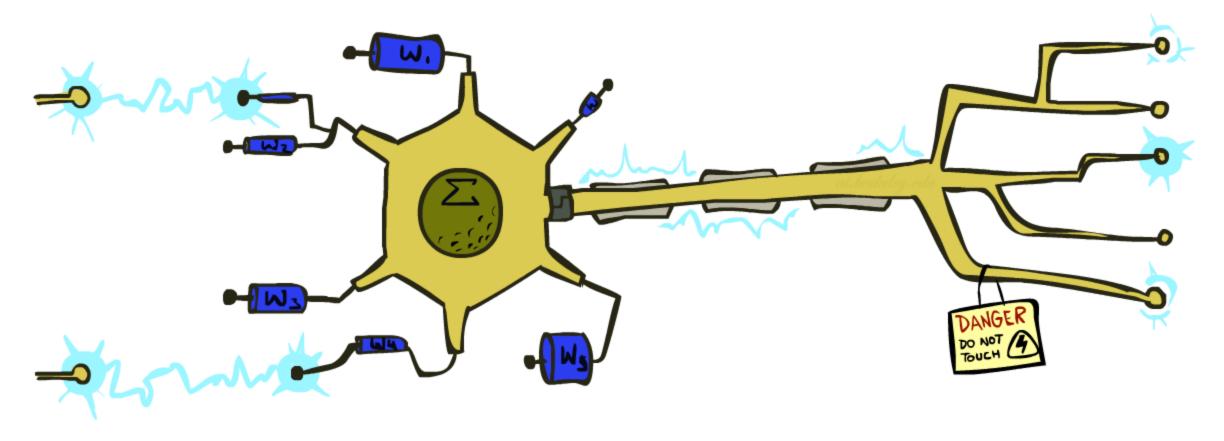
# CSCI 446: Artificial Intelligence

Perceptrons



Instructor: Michele Van Dyne

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

# Outline

- Error Driven Classification
- Linear Classifiers
- Weight Updates
- Improving the Perceptron

#### **Error-Driven Classification**



#### Errors, and What to Do

#### Examples of errors

Dear GlobalSCAPE Customer,

GlobalSCAPE has partnered with ScanSoft to offer you the latest version of OmniPage Pro, for just \$99.99\* - the regular list price is \$499! The most common question we've received about this offer is - Is this genuine? We would like to assure you that this offer is authorized by ScanSoft, is genuine and valid. You can get the . . .

. . . To receive your \$30 Amazon.com promotional certificate, click through to

http://www.amazon.com/apparel

and see the prominent link for the \$30 offer. All details are there. We hope you enjoyed receiving this message. However, if you'd rather not receive future e-mails announcing new store launches, please click . . .

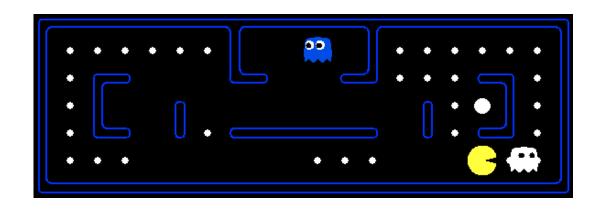
# What to Do About Errors

- Problem: there's still spam in your inbox
- Need more features words aren't enough!
  - Have you emailed the sender before?
  - Have 1M other people just gotten the same email?
  - Is the sending information consistent?
  - Is the email in ALL CAPS?
  - Do inline URLs point where they say they point?
  - Does the email address you by (your) name?
- Naïve Bayes models can incorporate a variety of features, but tend to do best in homogeneous cases (e.g. all features are word occurrences)

#### Later On...

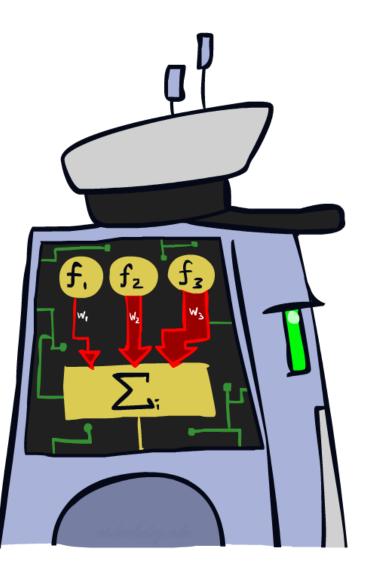


| Google  |                                   |
|---|-----------------------------------|
| Google Search I'm Feeling Lucky   | Advanced Search<br>Language Tools |
| Advertising Programs - Business Solutions - About Google<br>©2009 - Privacy |                                   |

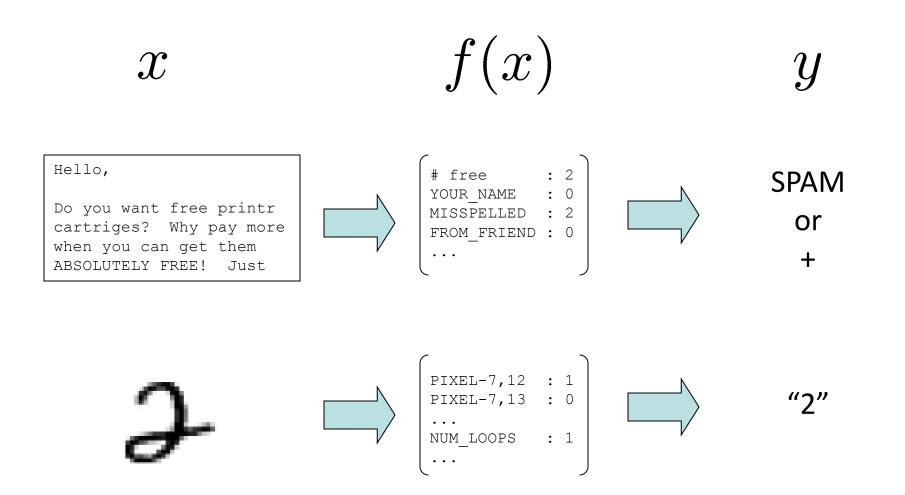


**Decision Problems** 

### **Linear Classifiers**

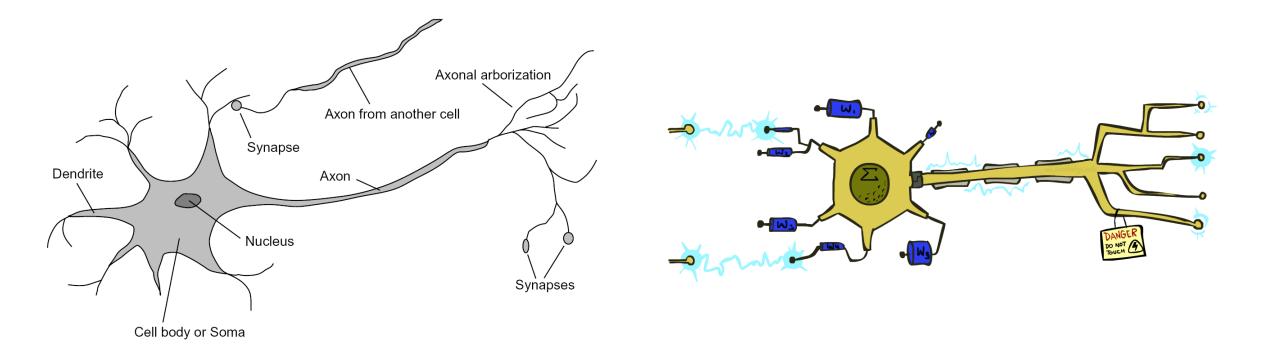


#### **Feature Vectors**



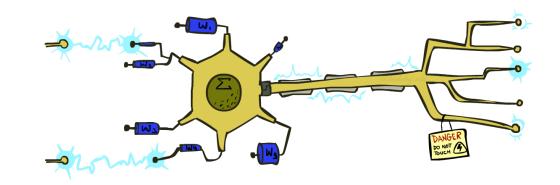
# Some (Simplified) Biology

#### Very loose inspiration: human neurons



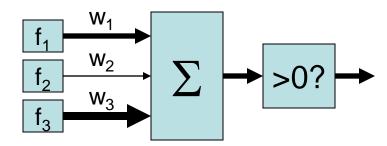
# **Linear Classifiers**

- Inputs are feature values
- Each feature has a weight
- Sum is the activation



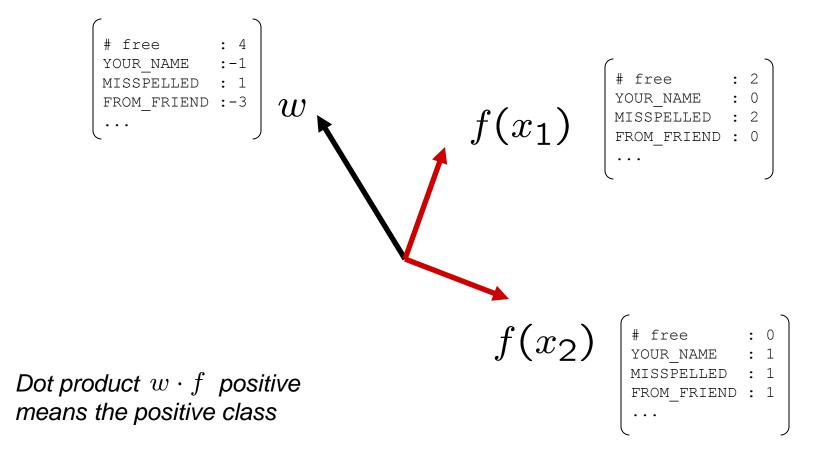
activation<sub>w</sub>(x) = 
$$\sum_{i} w_i \cdot f_i(x) = w \cdot f(x)$$

- If the activation is:
  - Positive, output +1
  - Negative, output -1

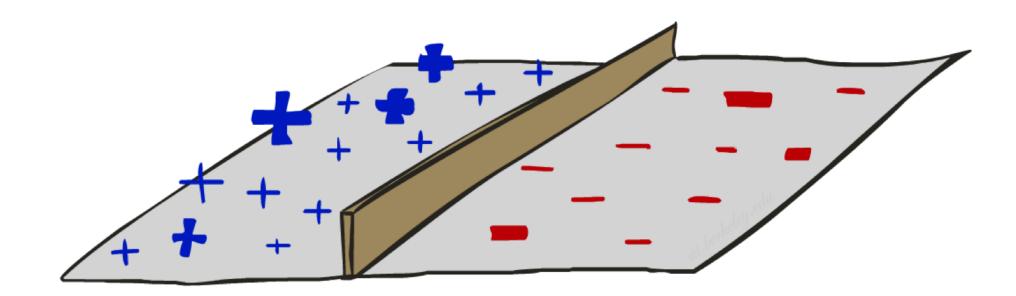


# Weights

- Binary case: compare features to a weight vector
- Learning: figure out the weight vector from examples

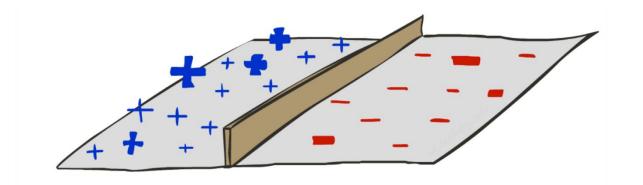


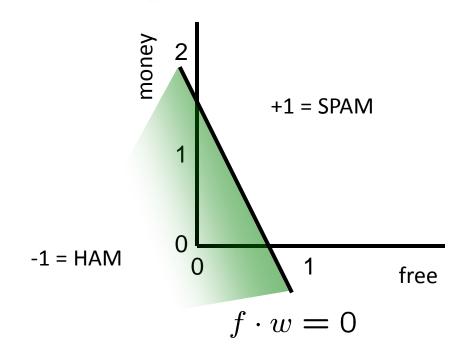
## **Decision Rules**



# **Binary Decision Rule**

- In the space of feature vectors
  - Examples are points
  - Any weight vector is a hyperplane
  - One side corresponds to Y=+1
  - Other corresponds to Y=-1





w

| -     |   |    |
|-------|---|----|
| BIAS  | : | -3 |
| free  | : | 4  |
| money | : | 2  |
| • • • |   |    |

# Weight Updates

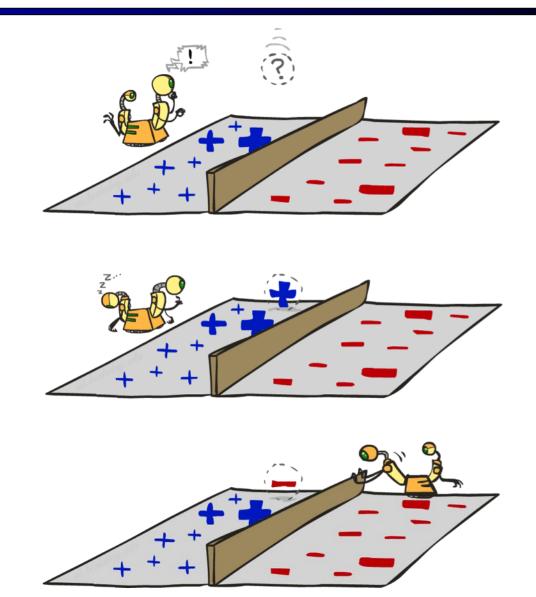


# Learning: Binary Perceptron

- Start with weights = 0
- For each training instance:
  - Classify with current weights

If correct (i.e., y=y\*), no change!

If wrong: adjust the weight vector



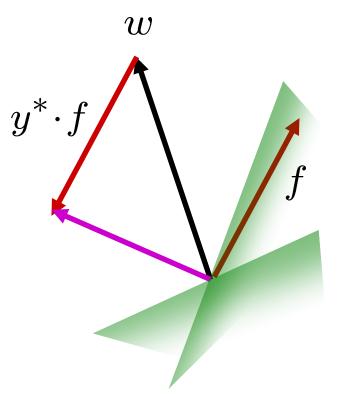
# Learning: Binary Perceptron

- Start with weights = 0
- For each training instance:
  - Classify with current weights

$$y = \begin{cases} +1 & \text{if } w \cdot f(x) \ge 0\\ -1 & \text{if } w \cdot f(x) < 0 \end{cases}$$

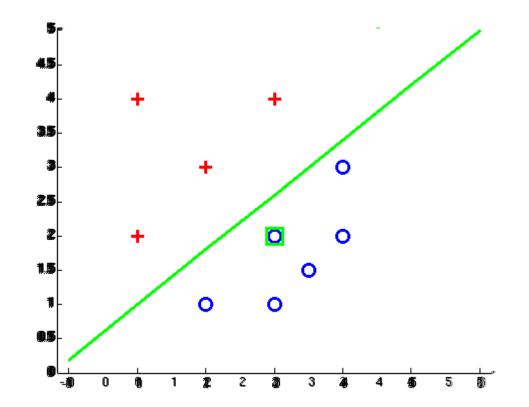
- If correct (i.e., y=y\*), no change!
- If wrong: adjust the weight vector by adding or subtracting the feature vector. Subtract if y\* is -1.

$$w = w + y^* \cdot f$$



### **Examples:** Perceptron

Separable Case



# **Multiclass Decision Rule**

- If we have multiple classes:
  - A weight vector for each class:

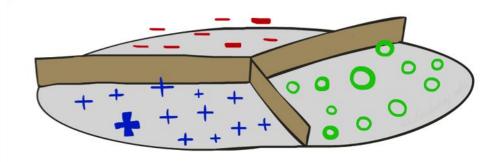
 $w_y$ 

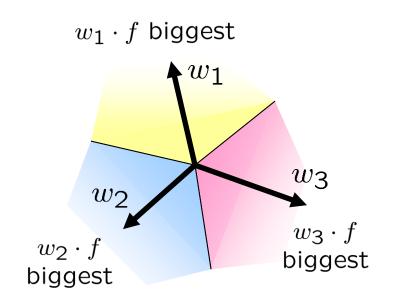
Score (activation) of a class y:

 $w_y \cdot f(x)$ 

Prediction highest score wins

$$y = \underset{y}{\operatorname{arg\,max}} w_y \cdot f(x)$$





Binary = multiclass where the negative class has weight zero

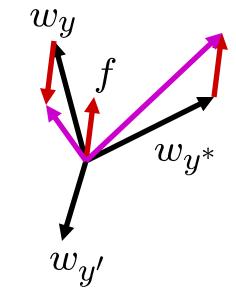
# Learning: Multiclass Perceptron

- Start with all weights = 0
- Pick up training examples one by one
- Predict with current weights

 $y = \arg \max_y w_y \cdot f(x)$ 

- If correct, no change!
- If wrong: lower score of wrong answer, raise score of right answer

$$w_y = w_y - f(x)$$
$$w_{y^*} = w_{y^*} + f(x)$$



## **Example: Multiclass Perceptron**

- "win the vote"
- "win the election"
- "win the game"

 $w_{SPORTS}$ 

| BIAS | • | 1 |  |
|------|---|---|--|
| win  | : | 0 |  |
| game | : | 0 |  |
| vote | : | 0 |  |
| the  | • | 0 |  |
| •••  |   |   |  |

#### *w*<sub>POLITICS</sub>

| $w_{TECH}$ |
|------------|
|------------|

| BIAS | : | 0 |  |
|------|---|---|--|
| win  | : | 0 |  |
| game | : | 0 |  |
| vote | : | 0 |  |
| the  | : | 0 |  |
| •••  |   |   |  |

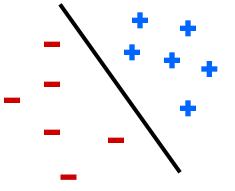
| BIAS | : | 0 |
|------|---|---|
| win  | : | 0 |
| game | : | 0 |
| vote | : | 0 |
| the  | : | 0 |
| •••  |   |   |

# **Properties of Perceptrons**

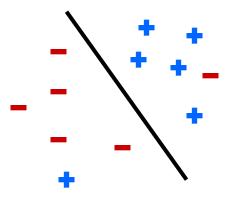
- Separability: true if some parameters get the training set perfectly correct
- Convergence: if the training is separable, perceptron will eventually converge (binary case)
- Mistake Bound: the maximum number of mistakes (binary case) related to the margin or degree of separability

mistakes 
$$< \frac{k}{\delta^2}$$



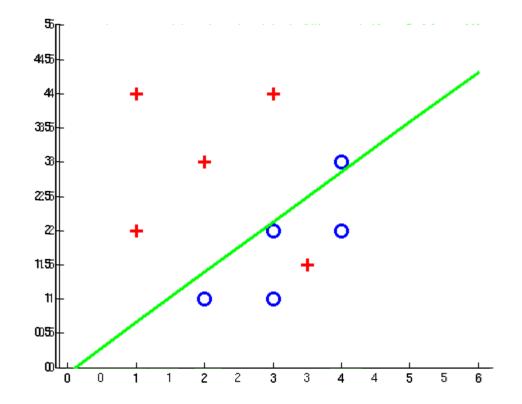


Non-Separable

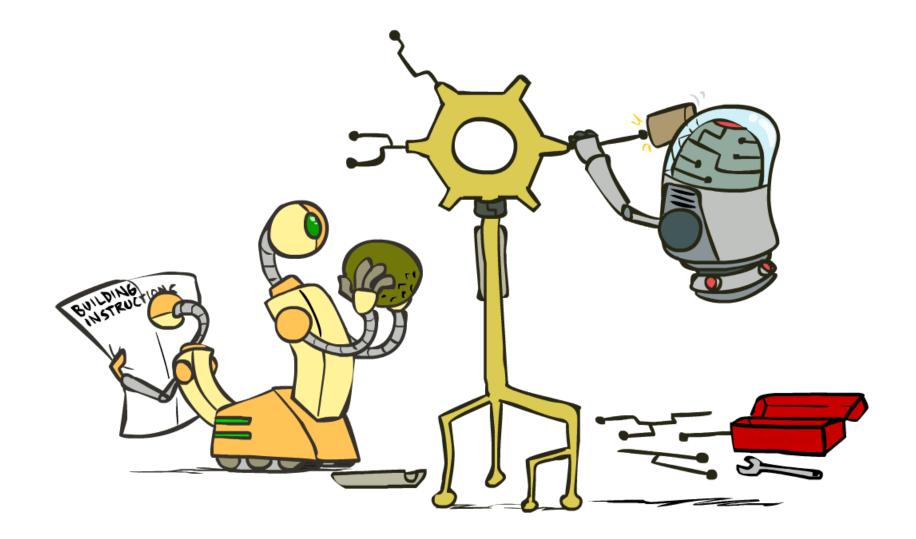


# **Examples:** Perceptron

Non-Separable Case



#### Improving the Perceptron

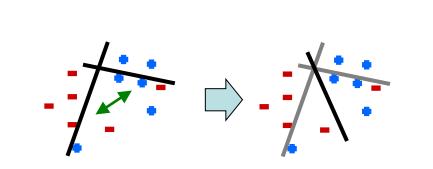


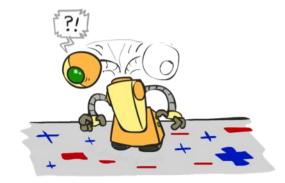
# Problems with the Perceptron

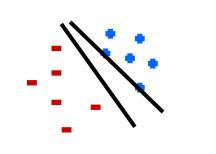
- Noise: if the data isn't separable, weights might thrash
  - Averaging weight vectors over time can help (averaged perceptron)

 Mediocre generalization: finds a "barely" separating solution

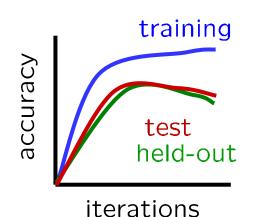
- Overtraining: test / held-out accuracy usually rises, then falls
  - Overtraining is a kind of overfitting













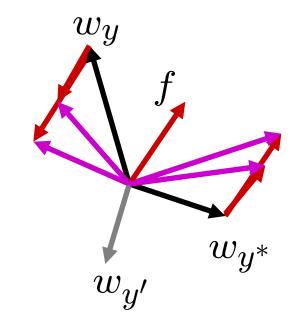
# Fixing the Perceptron

- Idea: adjust the weight update to mitigate these effects
- MIRA\*: choose an update size that fixes the current mistake...
- ... but, minimizes the change to w

$$\min_{w} \frac{1}{2} \sum_{y} ||w_y - w'_y||^2$$
$$w_{y^*} \cdot f(x) \ge w_y \cdot f(x) + 1$$

The +1 helps to generalize

\* Margin Infused Relaxed Algorithm

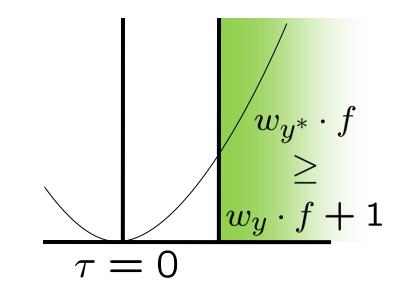


Guessed y instead of  $y^*$  on example x with features f(x)

$$w_y = w'_y - \tau f(x)$$
$$w_{y^*} = w'_{y^*} + \tau f(x)$$

#### Minimum Correcting Update

$$w_y = w'_y - \tau f(x)$$
$$w_{y^*} = w'_{y^*} + \tau f(x)$$

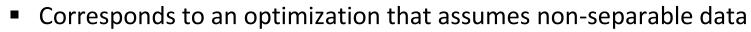


min not T=0, or would not have made an error, so min will be where equality holds

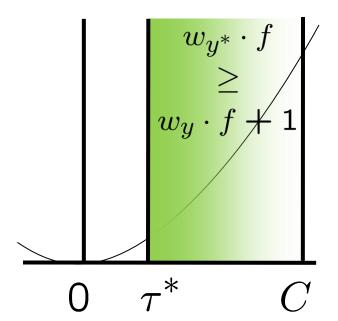
# Maximum Step Size

- In practice, it's also bad to make updates that are too large
  - Example may be labeled incorrectly
  - You may not have enough features
  - Solution: cap the maximum possible value of τ with some constant C

$$\tau^* = \min\left(\frac{(w'_y - w'_{y^*}) \cdot f + 1}{2f \cdot f}, C\right)$$

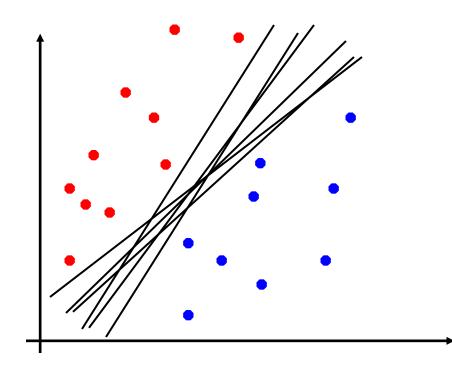


- Usually converges faster than perceptron
- Usually better, especially on noisy data



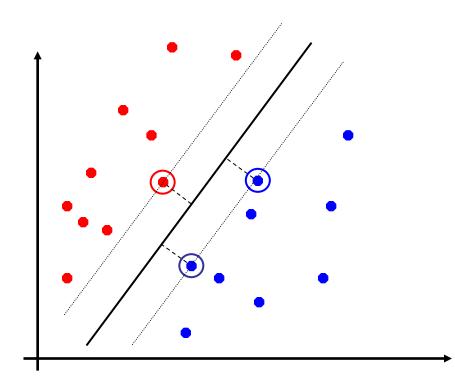
### **Linear Separators**

Which of these linear separators is optimal?



# **Support Vector Machines**

- Maximizing the margin: good according to intuition, theory, practice
- Only support vectors matter; other training examples are ignorable
- Support vector machines (SVMs) find the separator with max margin
- Basically, SVMs are MIRA where you optimize over all examples at once





$$\min_{w} \frac{1}{2} ||w - w'||^2$$
$$w_{y^*} \cdot f(x_i) \ge w_y \cdot f(x_i) + 1$$

SVM

$$\min_{w} \frac{1}{2} ||w||^2$$
  
$$\forall i, y \ w_{y^*} \cdot f(x_i) \ge w_y \cdot f(x_i) + 1$$

# **Classification:** Comparison

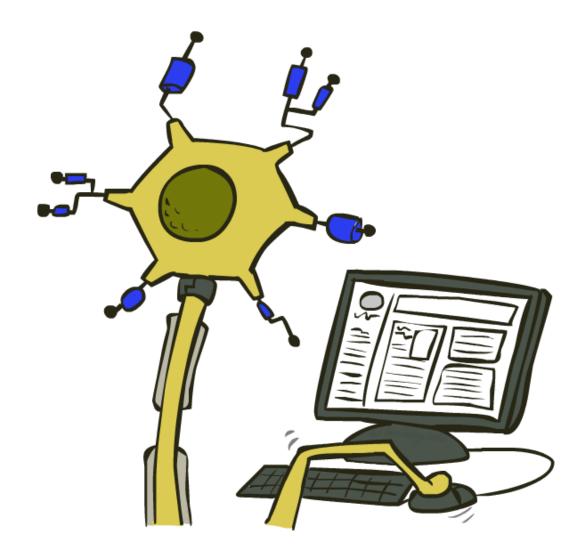
#### Naïve Bayes

- Builds a model training data
- Gives prediction probabilities
- Strong assumptions about feature independence
- One pass through data (counting)

#### Perceptrons / MIRA:

- Makes less assumptions about data
- Mistake-driven learning
- Multiple passes through data (prediction)
- Often more accurate

## Web Search



# **Extension: Web Search**

- Information retrieval:
  - Given information needs, produce information
  - Includes, e.g. web search, question answering, and classic IR
- Web search: not exactly classification, but rather ranking

#### *x* = "Apple Computers"



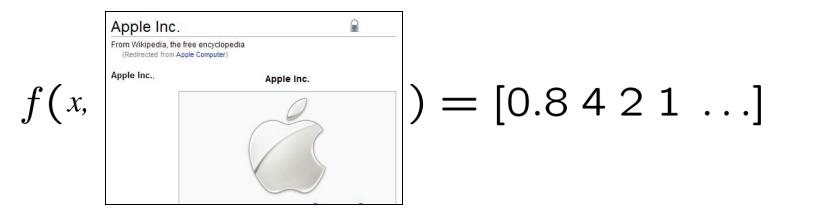
| Apple  |   |
|--|---|
| From Wikipedia, the free encyclopedia  |   |
| This article is about the fruit. For the see Apple Inc For other uses, see   | e electronics and software company<br>Apple (disambiguation). |
| The apple is the pomaceous fruit of  | Apple   |
| the apple tree, species Malus<br>domestica in the rose family                | A 10 -488   |
| Rosaceae. It is one of the most widely                                       | · · · · · ·   |
| cultivated tree fruits. The tree is small                                    | Mr. Mr.   |
| and deciduous, reaching 3 to 12<br>metres (9.8 to 39 ft) tall, with a broad, | 1 State 1   |
| often densely twiggy crown. <sup>[1]</sup> The                               |   |
| leaves are alternately arranged simple                                       | 1010 - 31A  |

#### **Feature-Based Ranking**

#### *x* = "Apple Computer"



) = [0.3500...]



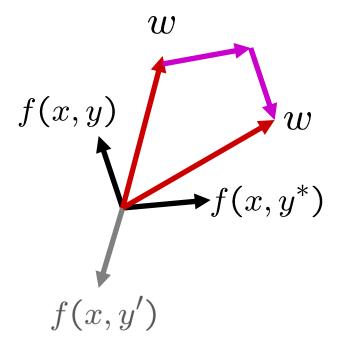
# Perceptron for Ranking

- Inputs x
- Candidates y
- Many feature vectors: f(x, y)
- One weight vector: w
  - Prediction:

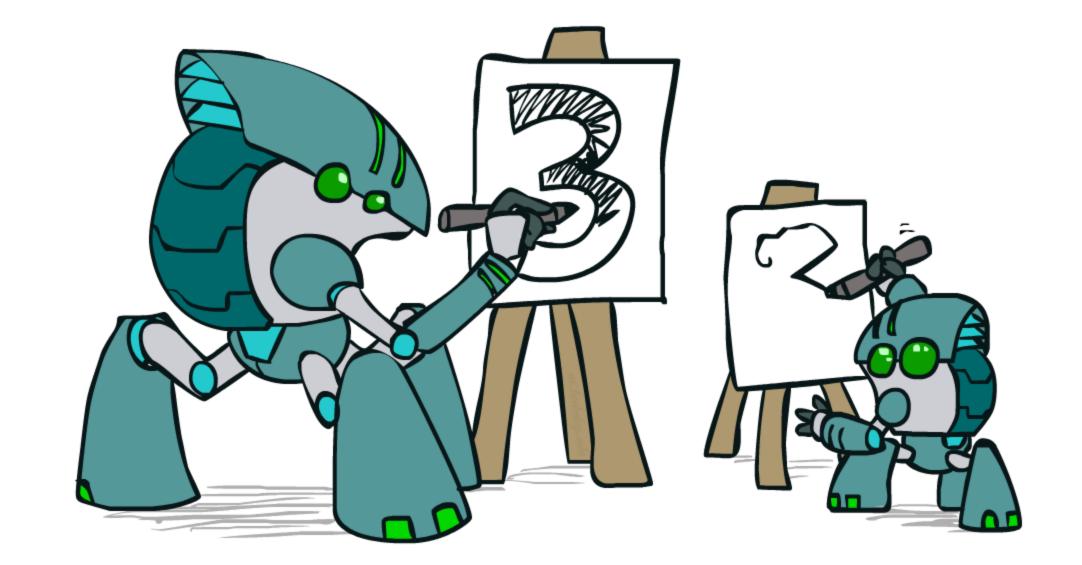
 $y = \arg \max_y w \cdot f(x, y)$ 

Update (if wrong):

$$w = w + f(x, y^*) - f(x, y)$$

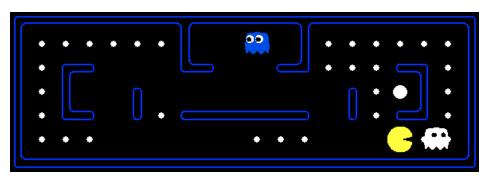


# Apprenticeship



# Pacman Apprenticeship!

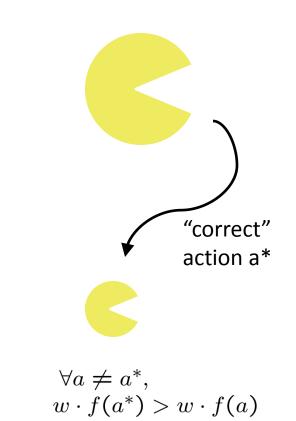
Examples are states s



- Candidates are pairs (s,a)
- "Correct" actions: those taken by expert
- Features defined over (s,a) pairs: f(s,a)
- Score of a q-state (s,a) given by:

$$w \cdot f(s, a)$$

How is this VERY different from reinforcement learning?



# Summary

- Error Driven Classification
- Linear Classifiers
- Weight Updates
- Improving the Perceptron

