

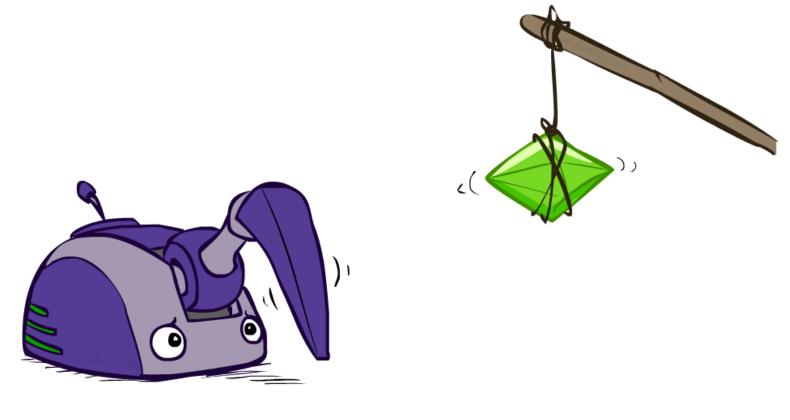
Instructor: Michele Van Dyne

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

Today

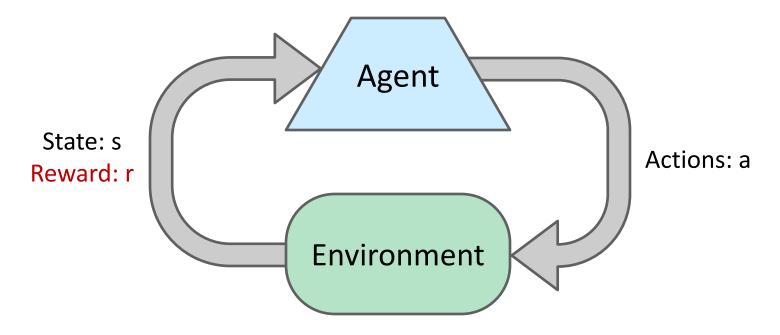
- Reinforcement Learning
- Offline (MDPs) vs Online (RL)
 - Model-Based Learning
 - Model-Free Learning
 - Passive Reinforcement Learning
 - Temporal Difference Learning
 - Active Reinforcement Learning

Reinforcement Learning





Reinforcement Learning



- Basic idea:
 - Receive feedback in the form of rewards
 - Agent's utility is defined by the reward function
 - Must (learn to) act so as to maximize expected rewards
 - All learning is based on observed samples of outcomes!



Initial



A Learning Trial



After Learning [1K Trials]



Initial

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – initial]



Training

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – training]



Finished

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – finished]

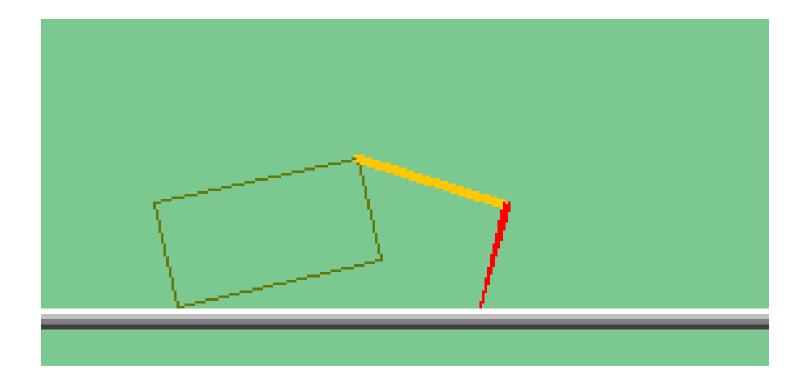
Example: Toddler Robot



[Tedrake, Zhang and Seung, 2005]

[Video: TODDLER – 40s]

The Crawler!



[Demo: Crawler Bot (L10D1)] [You, in Project 3]

Reinforcement Learning

- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model T(s,a,s')
 - A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$



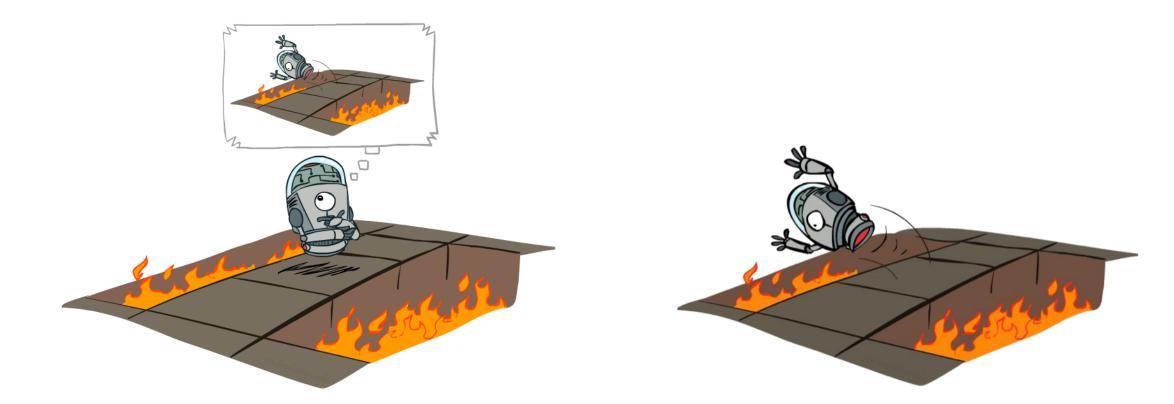




Overheated

- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try actions and states out to learn

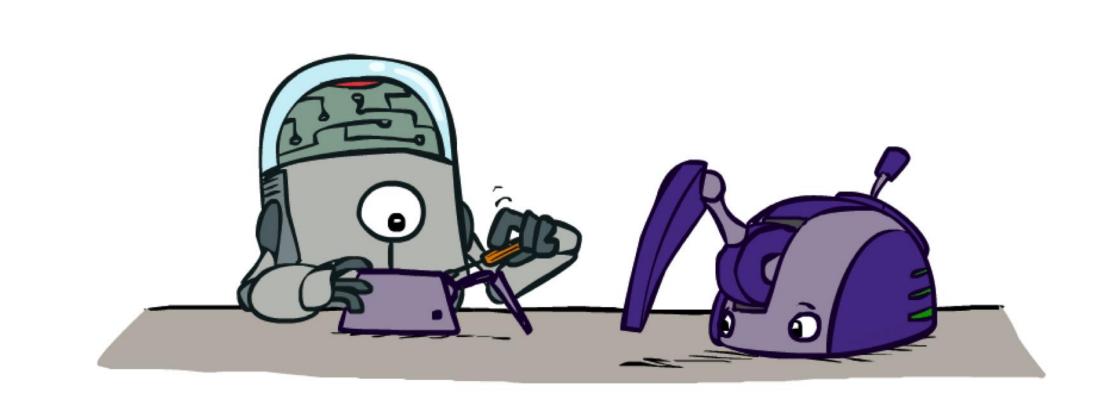
Offline (MDPs) vs. Online (RL)



Offline Solution

Online Learning

Model-Based Learning



Model-Based Learning

Model-Based Idea:

- Learn an approximate model based on experiences
- Solve for values as if the learned model were correct

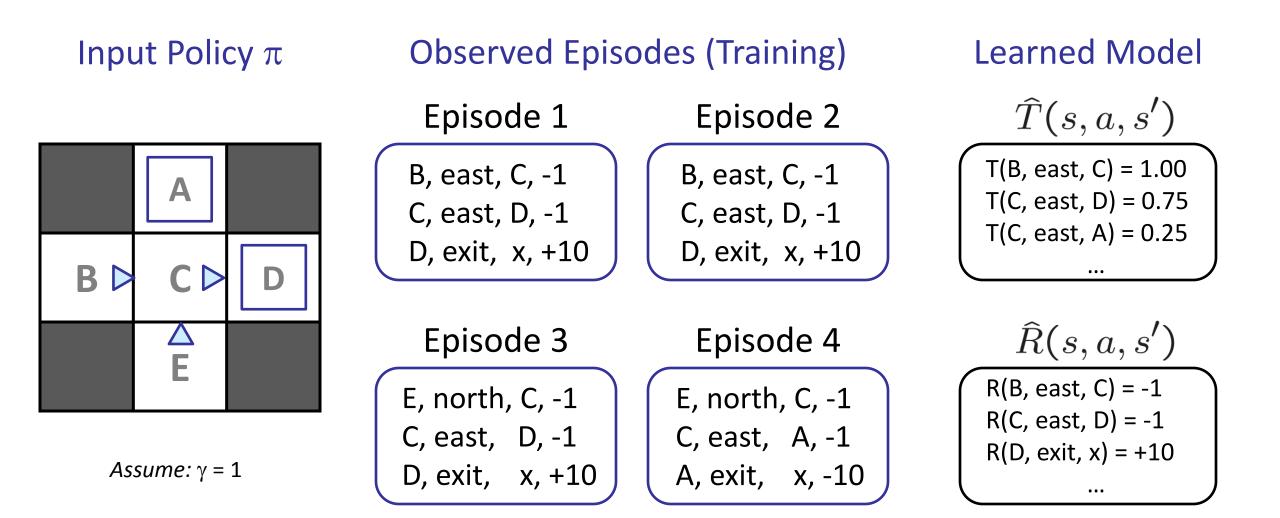
Step 1: Learn empirical MDP model

- Count outcomes s' for each s, a
- Normalize to give an estimate of $\widehat{T}(s, a, s')$
- Discover each $\widehat{R}(s, a, s')$ when we experience (s, a, s')
- Step 2: Solve the learned MDP
 - For example, use value iteration, as before



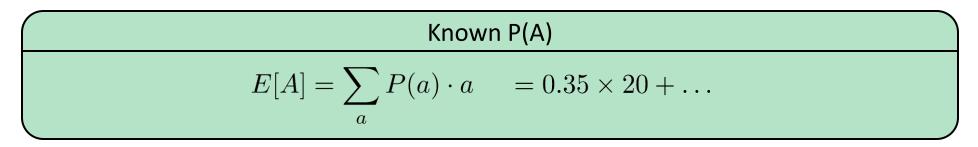


Example: Model-Based Learning

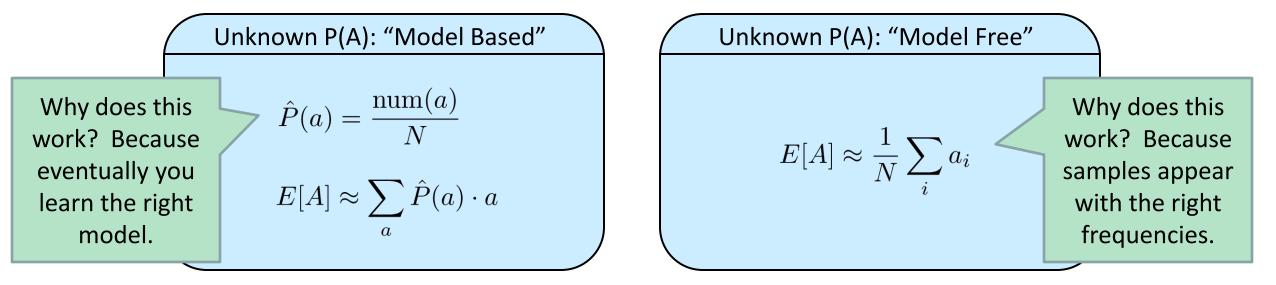


Example: Expected Age

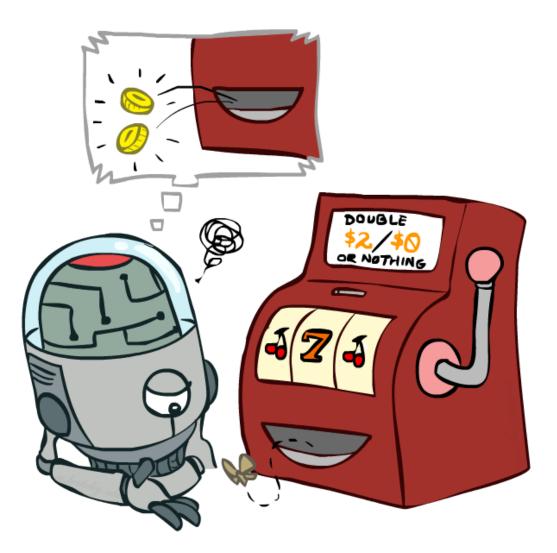
Goal: Compute expected age of CSCI 446 students



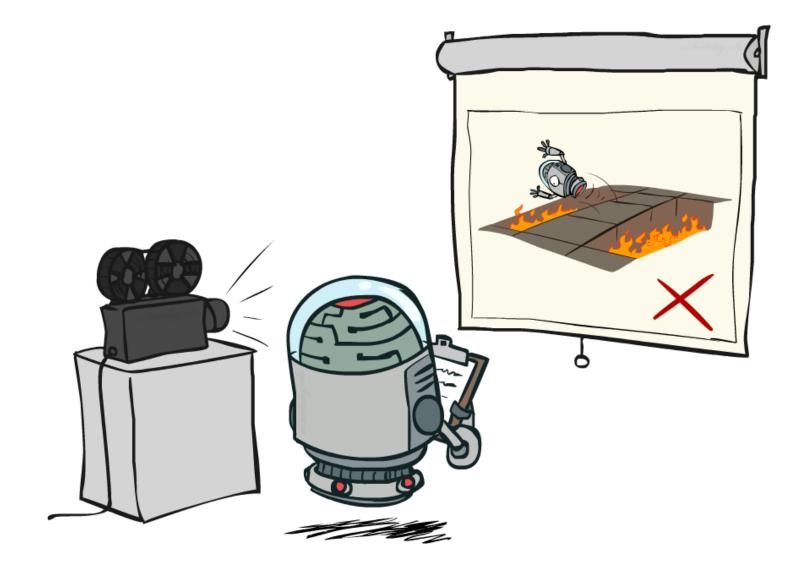
Without P(A), instead collect samples $[a_1, a_2, ..., a_N]$



Model-Free Learning



Passive Reinforcement Learning



Passive Reinforcement Learning

Simplified task: policy evaluation

- Input: a fixed policy π(s)
- You don't know the transitions T(s,a,s')
- You don't know the rewards R(s,a,s')
- Goal: learn the state values

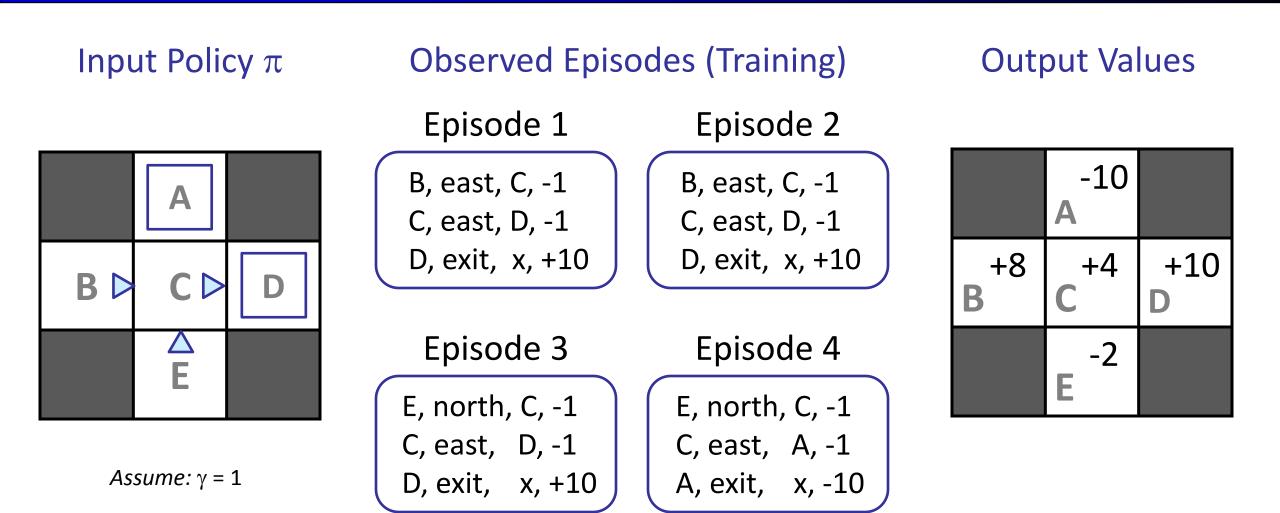
- In this case:
 - Learner is "along for the ride"
 - No choice about what actions to take
 - Just execute the policy and learn from experience
 - This is NOT offline planning! You actually take actions in the world.

Direct Evaluation

- Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be
 - Average those samples
- This is called direct evaluation



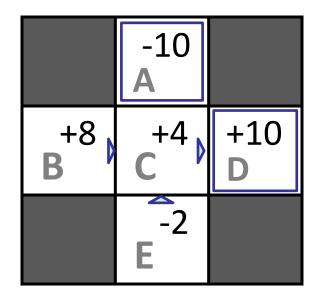
Example: Direct Evaluation



Problems with Direct Evaluation

- What's good about direct evaluation?
 - It's easy to understand
 - It doesn't require any knowledge of T, R
 - It eventually computes the correct average values, using just sample transitions
- What bad about it?
 - It wastes information about state connections
 - Each state must be learned separately
 - So, it takes a long time to learn

Output Values



If B and E both go to C under this policy, how can their values be different?

Why Not Use Policy Evaluation?

π(s)

s, π(s),s'

- Simplified Bellman updates calculate V for a fixed policy:
 - Each round, replace V with a one-step-look-ahead layer over V

$$V_0^{\pi}(s) = 0$$

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
 - In other words, how to we take a weighted average without knowing the weights?

Sample-Based Policy Evaluation?

We want to improve our estimate of V by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

Idea: Take samples of outcomes s' (by doing the action!) and average

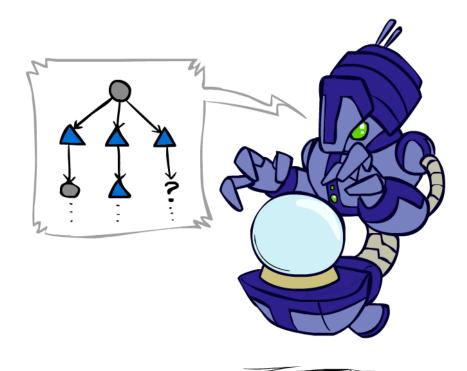
$$sample_{1} = R(s, \pi(s), s_{1}') + \gamma V_{k}^{\pi}(s_{1}')$$

$$sample_{2} = R(s, \pi(s), s_{2}') + \gamma V_{k}^{\pi}(s_{2}')$$

$$\dots$$

$$sample_{n} = R(s, \pi(s), s_{n}') + \gamma V_{k}^{\pi}(s_{n}')$$

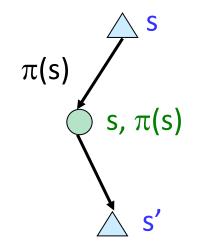
$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_{i} sample_{i}$$



Temporal Difference Learning

- Big idea: learn from every experience!
 - Update V(s) each time we experience a transition (s, a, s', r)
 - Likely outcomes s' will contribute updates more often
- Temporal difference learning of values
 - Policy still fixed, still doing evaluation!
 - Move values toward value of whatever successor occurs: running average

Sample of V(s): $sample = R(s, \pi(s), s') + \gamma V^{\pi}(s')$ Update to V(s): $V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + (\alpha)sample$ Same update: $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$



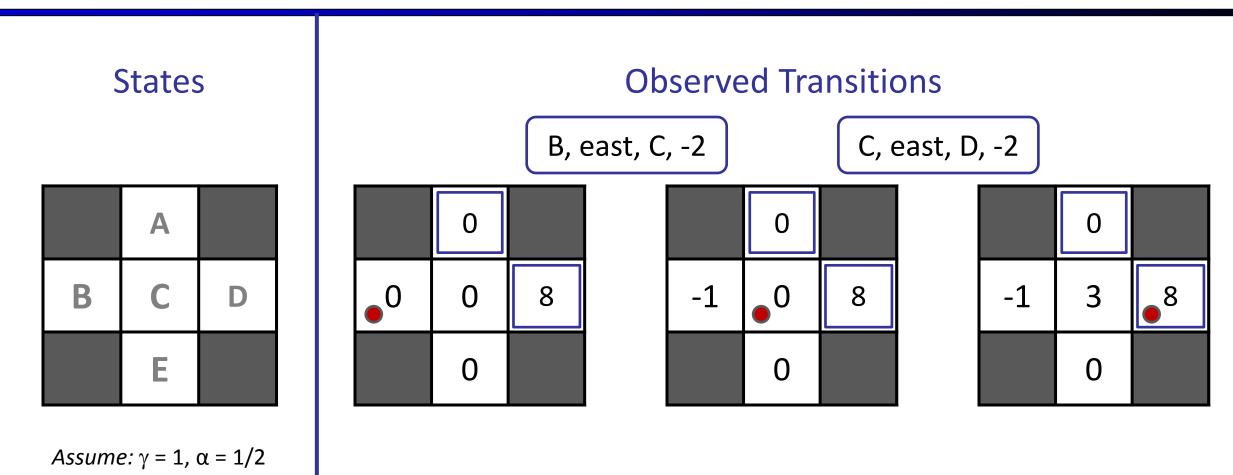
Exponential Moving Average

- Exponential moving average
 - The running interpolation update: $\bar{x}_n = (1 \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$
 - Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages

Example: Temporal Difference Learning



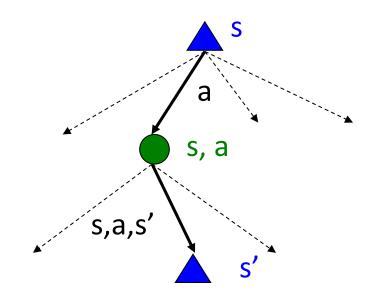
 $V^{\pi}(s) \leftarrow (1-\alpha)V^{\pi}(s) + \alpha \left[R(s,\pi(s),s') + \gamma V^{\pi}(s') \right]$

Problems with TD Value Learning

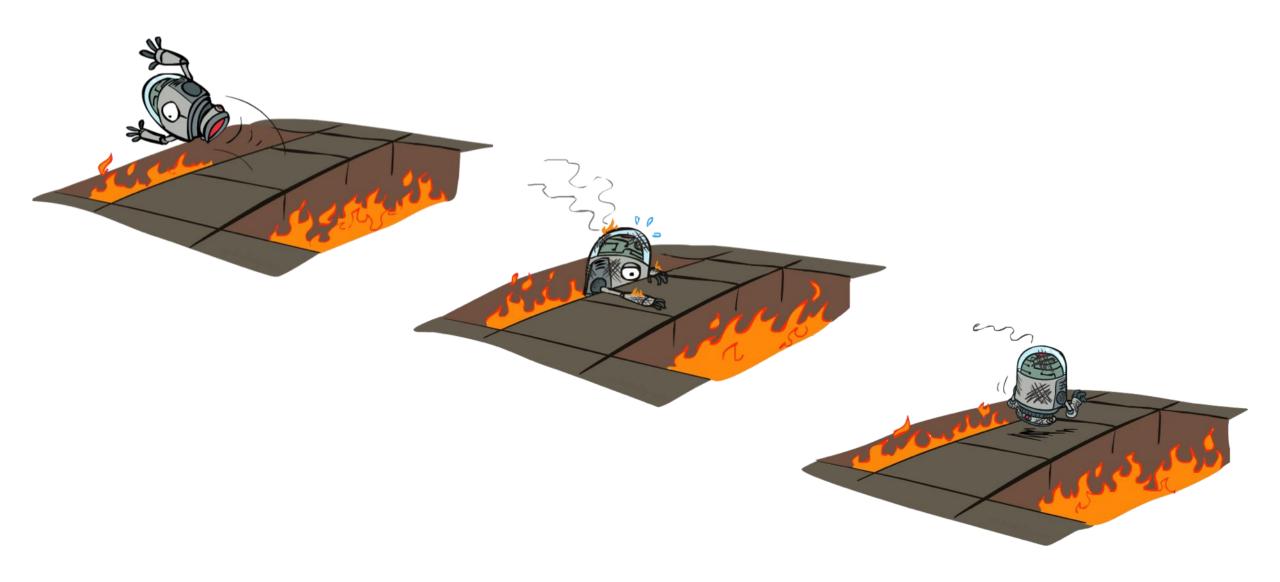
- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

 $\pi(s) = \arg\max_{a} Q(s, a)$ $Q(s, a) = \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V(s') \right]$

- Idea: learn Q-values, not values
- Makes action selection model-free too!



Active Reinforcement Learning

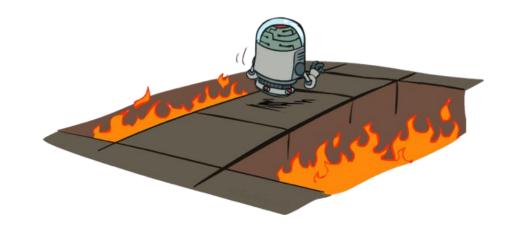


Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - You choose the actions now
 - Goal: learn the optimal policy / values

In this case:

- Learner makes choices!
- Fundamental tradeoff: exploration vs. exploitation
- This is NOT offline planning! You actually take actions in the world and find out what happens...



Detour: Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 - Start with V₀(s) = 0, which we know is right
 - Given V_k, calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
 - Start with Q₀(s,a) = 0, which we know is right
 - Given Q_k, calculate the depth k+1 q-values for all q-states:

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

Q-Learning

Q-Learning: sample-based Q-value iteration

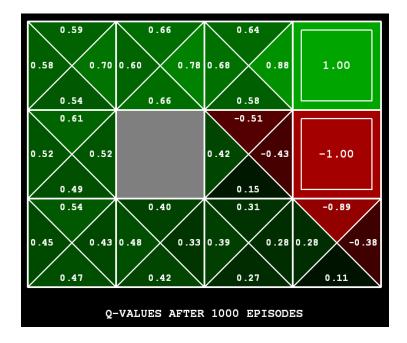
$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

- Learn Q(s,a) values as you go
 - Receive a sample (s,a,s',r)
 - Consider your old estimate: Q(s, a)
 - Consider your new sample estimate:

 $sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$

Incorporate the new estimate into a running average:

 $Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) [sample]$



[Demo: Q-learning – gridworld (L10D2)] [Demo: Q-learning – crawler (L10D3)]

Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
 - You have to explore enough
 - You have to eventually make the learning rate small enough
 - ... but not decrease it too quickly
 - Basically, in the limit, it doesn't matter how you select actions (!)



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