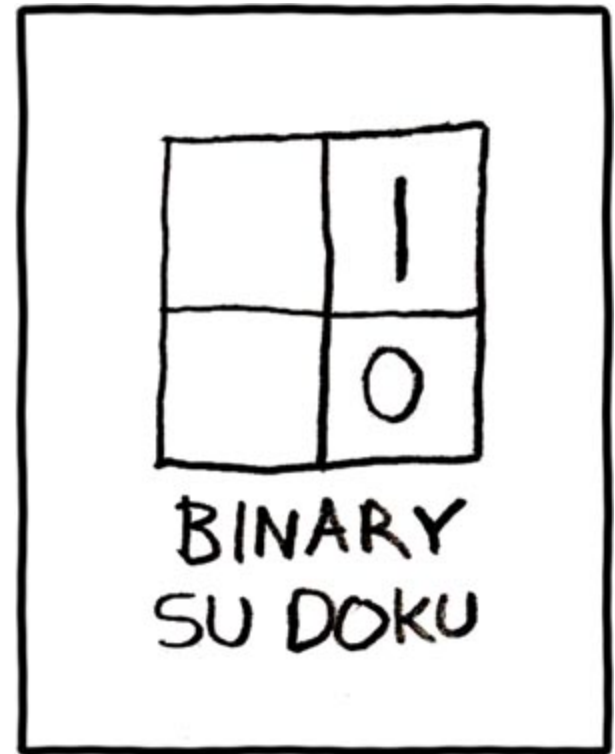
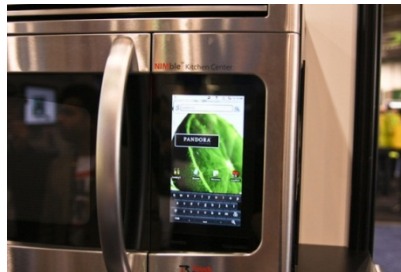


Embedded systems intro, Number systems



<http://xkcd.com/74/>

Overview

- What exactly is an *embedded system*?
- *Why study* embedded systems?
- Number systems
 - Base 2, 8, 10, 16
 - Converting between them all

General-purpose computer



- Device with a microprocessor
- Jack of all trades
- People willing to pay big \$\$\$
- Rich input/output
- Crashing is irritating
- Complex operating system
- Lots of memory
- Powerful processor
- Program in high level languages ignoring hardware details

Embedded system



- Device with a microprocessor
- Specialize in 1 or a few things
- Must be very cheap
- Little to no input/output
- Crashing could kill somebody
- Often no operating system
- Little memory
- Simple processor
- Program “to the metal” often in low level languages (e.g. assembly)

General-purpose computer



1%

Embedded system



99%

Blurred lines?



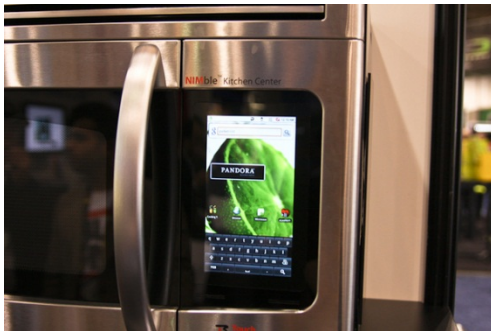
LG VX5600



iPhone 4



Nokia 810



Android microwave



Android washing machine

Why study embedded?

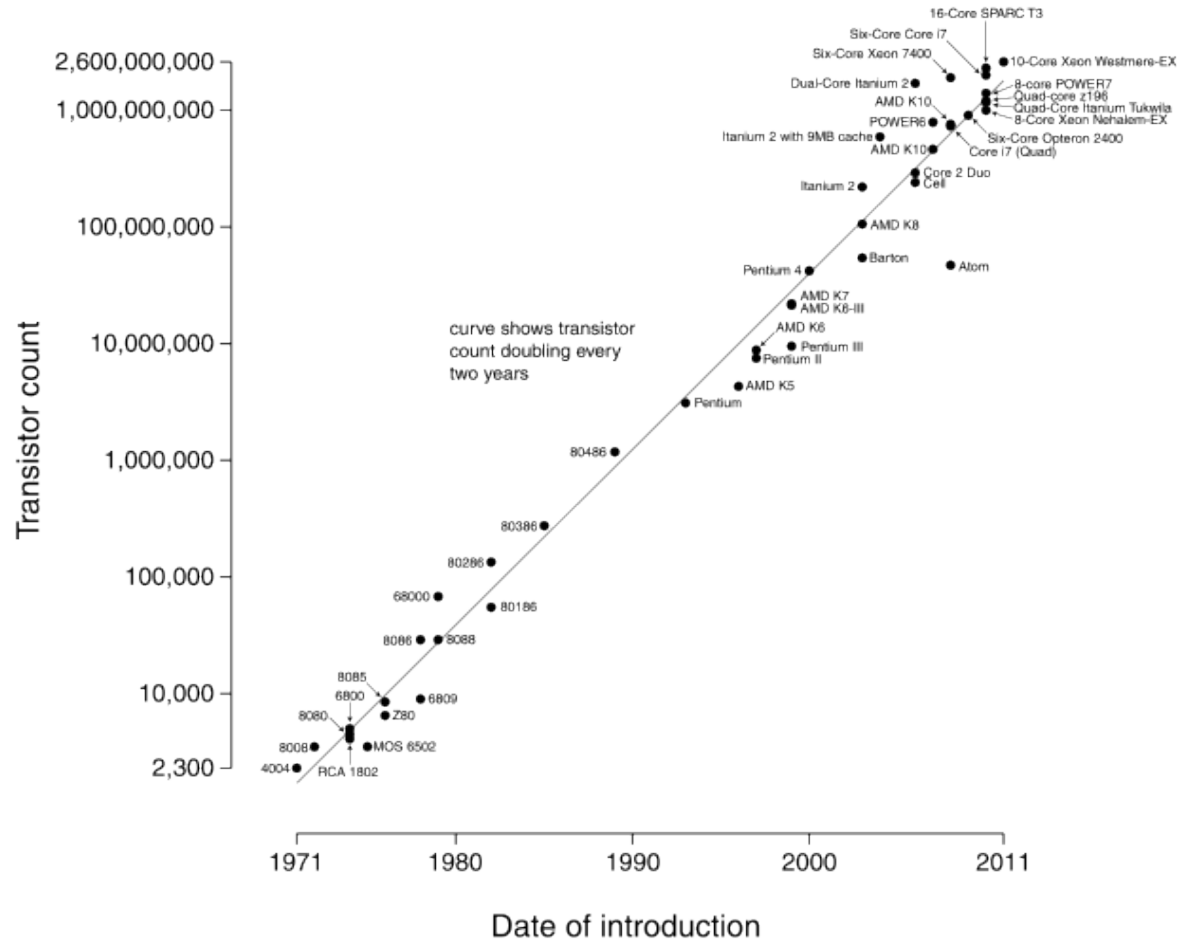
- Opens up the other 99% of microprocessors
- **Learn how computers work** from ground up
- Prepare you for more advanced computer architecture courses
 - Binary, octal, hexadecimal **number systems**
 - How computers **store numbers**
 - **Bitwise operations**
 - **Boolean algebra**
 - Combinational and sequential **circuits**
 - How computers **fetch and execute** instructions

Why study embedded?

- Gain **assembly language** experience
 - Makes you **appreciate high-level languages**
 - Understand underlying **hardware realities**
 - **Programming simple processors** with no memory/
cycles to waste
 - **Extreme optimization** of certain portions of a program
(e.g. frequent calculations)
 - Modern optimizing compilers make gains questionable
 - Interacting directly with hardware (e.g. **device drivers**)
 - Real-time programs needing **precise timing**

Where have all the simple processors gone?

Microprocessor Transistor Counts 1971-2011 & Moore's Law



Real-time

- **Soft real-time** - respond to a click in 100 ms
- **Hard real-time** - respond to rudder correction in 100 ms
- **Timing unpredictable in high-level languages & operating systems**
 - Java garbage collection
 - Thread scheduling by OS
 - Windows update
- **Real-time versions of languages & operating systems**
 - Real-time Java, real-time Linux, Windows CE

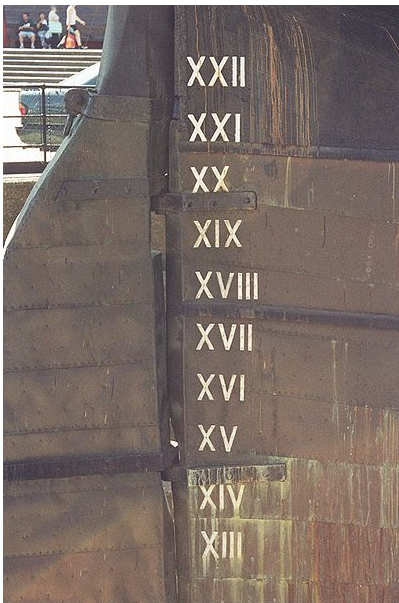
Embedded development challenges

- Reliability
 - **Cannot crash**, devices often run 24 x 7 x 365
 - Thorough testing, must handle errors and unexpected events
- Performance
 - **Real time** systems, rapid response
 - Antilock brakes → detect slippage and react within ms
 - Must not be bottleneck, good throughput
 - Multitasking, **handle interrupts** when data arrives

Embedded development challenges

- Resource constraints
 - Cost of device
 - Amount of memory
 - Power consumption (huge for mobile devices)
- Debugging
 - Is this a software or hardware problem?
 - Easier than hardware circuits, harder than desktop
- User interface
 - One-off device with perhaps limit I/O capabilities
 - Users won't read manual

Number systems



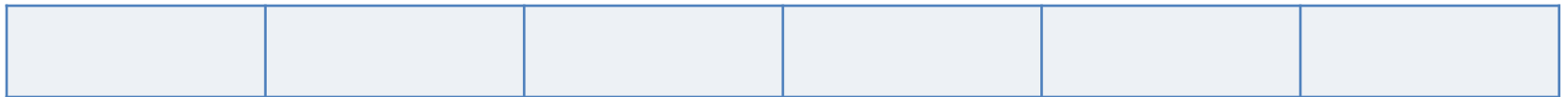
0	1	2	3	4
	•	••	•••	••••
5	6	7	8	9
—	•	••	•••	••••
10	11	12	13	14
— —	•	••	•••	••••
15	16	17	18	19
— — —	•	••	•••	••••

∩	1	∩∩	11	∩∩∩	21
∩∩	2	∩∩∩	12	∩∩∩∩	22
∩∩∩	3	∩∩∩∩	13	∩∩∩∩∩	23
∩∩∩∩	4	∩∩∩∩∩	14	∩∩∩∩∩∩	24
∩∩∩∩∩	5	∩∩∩∩∩∩	15	∩∩∩∩∩∩∩	25
∩∩∩∩∩∩	6	∩∩∩∩∩∩∩	16	∩∩∩∩∩∩∩∩	26
∩∩∩∩∩∩∩	7	∩∩∩∩∩∩∩∩	17	∩∩∩∩∩∩∩∩∩	27
∩∩∩∩∩∩∩∩	8	∩∩∩∩∩∩∩∩∩	18	∩∩∩∩∩∩∩∩∩∩	28
∩∩∩∩∩∩∩∩∩	9	∩∩∩∩∩∩∩∩∩∩	19	∩∩∩∩∩∩∩∩∩∩∩	29
∩	10	∩∩	20	∩∩∩	30

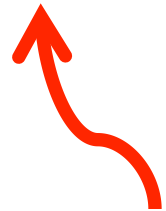
Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:



Most significant



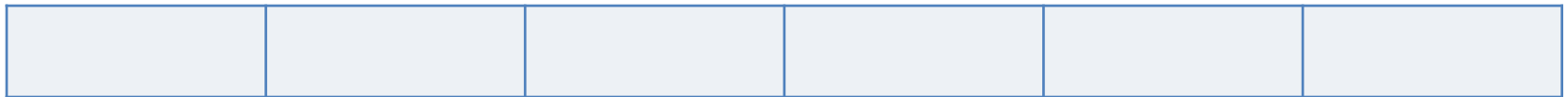
Least significant

Our friend: base 10

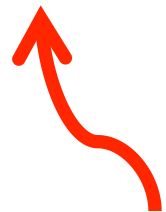


- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$



Most significant



Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

0					
---	--	--	--	--	--

$$1252 - 0 \cdot 100000 = 1252$$

Most significant

Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

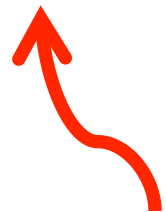
0	0				
---	---	--	--	--	--



Most significant

$$1252 - 0 \cdot 100000 = 1252$$

$$1252 - 0 \cdot 10000 = 1252$$



Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

0	0	1			
---	---	---	--	--	--

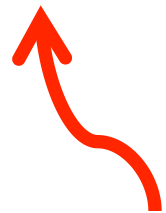


Most significant

$$1252 - 0 \cdot 100000 = 1252$$

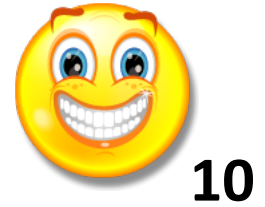
$$1252 - 0 \cdot 10000 = 1252$$

$$1252 - 1 \cdot 1000 = 252$$



Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

0	0	1	2		
---	---	---	---	--	--


Most significant

$$1252 - 0 \cdot 100000 = 1252$$

$$1252 - 0 \cdot 10000 = 1252$$

$$1252 - 1 \cdot 1000 = 252$$

$$252 - 2 \cdot 100 = 52$$


Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

0	0	1	2	5	
---	---	---	---	---	--


Most significant

$$1252 - 0 \cdot 100000 = 1252$$

$$1252 - 0 \cdot 10000 = 1252$$

$$1252 - 1 \cdot 1000 = 252$$

$$252 - 2 \cdot 100 = 52$$

$$52 - 5 \cdot 10 = 2$$


Least significant

Our friend: base 10



- “one thousand two hundred fifty two”
- Let’s convert this to 6-digit base 10:

$10^5=100000$ $10^4=10000$ $10^3=1000$ $10^2=100$ $10^1=10$ $10^0=1$

0	0	1	2	5	2
---	---	---	---	---	---


Most significant

$$1252 - 0 \cdot 100000 = 1252$$

$$1252 - 0 \cdot 10000 = 1252$$

$$1252 - 1 \cdot 1000 = 252$$

$$252 - 2 \cdot 100 = 52$$

$$52 - 5 \cdot 10 = 2$$

$$2 - 2 \cdot 1 = 0$$


Least significant

Our geeky friend: base 2



- Binary = base 2
- 0s and 1s
- low voltage (0-1V) vs. high voltage (3-5V)

01100111

0101

Our geeky friend: base 2



- Binary = base 2
- 0s and 1s
- low voltage (0-1V) vs. high voltage (3-5V)

01100111



8 bits = byte

0101

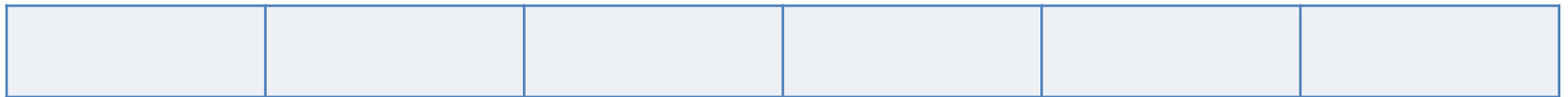


4 bits = nibble

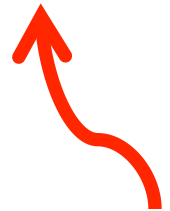
Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:



Most significant



Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

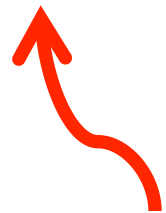
$2^1=2$

$2^0=1$

--	--	--	--	--	--



Most significant



Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

1					
---	--	--	--	--	--

$42 - 1 \cdot 32 = 10$

Most significant

Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

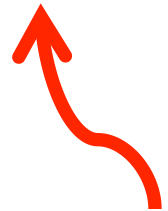
1	0				
---	---	--	--	--	--



Most significant

$$42 - 1 \cdot 32 = 10$$

$$10 - 0 \cdot 16 = 10$$



Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

1	0	1			
---	---	---	--	--	--



Most significant

$42 - 1 \cdot 32 = 10$

$10 - 0 \cdot 16 = 10$

$10 - 1 \cdot 8 = 2$



Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

1	0	1	0		
---	---	---	---	--	--

Most significant

$42 - 1 \cdot 32 = 10$

$10 - 0 \cdot 16 = 10$

$10 - 1 \cdot 8 = 2$

$2 - 0 \cdot 4 = 2$

Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

1	0	1	0	1	
---	---	---	---	---	--

Most significant

$42 - 1 \cdot 32 = 10$

$10 - 0 \cdot 16 = 10$

$10 - 1 \cdot 8 = 2$

$2 - 0 \cdot 4 = 2$

$2 - 1 \cdot 2 = 0$

Least significant

Our geeky friend: base 2



- “forty two”
- Let’s convert this to 6-digit base 2:

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

1	0	1	0	1	0
---	---	---	---	---	---

Most significant

$42 - 1 \cdot 32 = 10$

$10 - 0 \cdot 16 = 10$

$10 - 1 \cdot 8 = 2$

$2 - 0 \cdot 4 = 2$

$2 - 1 \cdot 2 = 0$

$0 - 0 \cdot 1 = 0$

Least significant

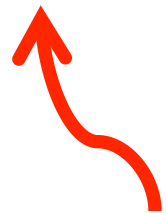
Our geeky friend: base 2



- Given a binary number: 011100
- What is this number in base 10?



Most significant



Least significant

Our geeky friend: base 2



- Given a binary number: 011100
- What is this number in base 10?

$2^5=32$

$2^4=16$

$2^3=8$

$2^2=4$

$2^1=2$

$2^0=1$

0	1	1	1	0	0
---	---	---	---	---	---

$16 + 8 + 4 = 28$

Most significant

Least significant

1110 0101 1010 0111

Our super geeky friend: base 16



16

1110 0101 1010 0111

E 5 A 7

- Hexadecimal (or hex)
- 16 digits: 0 1 2 3 4 5 6 7 8 9 **A B C D E F**
- Often written: 0xE5A7



Our super geeky friend: base 16



16

Binary : 1110 0101 1010 0111

Decimal : 58791

Hex : ?

$16^3=4096$

$16^2=256$

$16^1=16$

$16^0=1$

--	--	--	--

Our super geeky friend: base 16



16

Binary : 1110 0101 1010 0111

Decimal : 58791

Hex : E

$16^3=4096$

$16^2=256$

$16^1=16$

$16^0=1$

E			
----------	--	--	--

$$58791 - 14 \cdot 4096 = 1447$$

Our super geeky friend: base 16



16

Binary : 1110 0101 1010 0111

Decimal : 58791

Hex : E5

$16^3=4096$

$16^2=256$

$16^1=16$

$16^0=1$

E	5		
----------	----------	--	--

$$58791 - 14 \cdot 4096 = 1447$$

$$1447 - 5 \cdot 256 = 167$$

Our super geeky friend: base 16



16

Binary : 1110 0101 1010 0111

Decimal : 58791

Hex : E5A

$16^3=4096$

$16^2=256$

$16^1=16$

$16^0=1$

E	5	A	
----------	----------	----------	--

$$58791 - 14 \cdot 4096 = 1447$$

$$1447 - 5 \cdot 256 = 167$$

$$167 - 10 \cdot 16 = 7$$

Our super geeky friend: base 16



16

Binary : 1110 0101 1010 0111

Decimal : 58791

Hex : E5A7

$16^3=4096$

$16^2=256$

$16^1=16$

$16^0=1$

E	5	A	7
----------	----------	----------	----------

$$58791 - 14 \cdot 4096 = 1447$$

$$1447 - 5 \cdot 256 = 167$$

$$167 - 10 \cdot 16 = 7$$

$$7 - 7 \cdot 1 = 0$$

Binary	Hex	Decimal
0000	0x0	0
0001	0x1	1
0010	0x2	2
0011	0x3	3
0100	0x4	4
0101	0x5	5
0110	0x6	6
0111	0x7	7
1000	0x8	8
1001	0x9	9
1010	0xA	10
1011	0xB	11
1100	0xC	12
1101	0xD	13
1110	0xE	14
1111	0xF	15

0100111101100101

“nibblize” ↓

0100 1111 0110 0101

**Lookup in
table** ↓

4 F 6 5

**(also works the other
way: hex to binary)**

Our fringe friend: base 8



Binary : 110100111

Decimal : 423

Octal : ???

- Octal has 8 digits:

0 1 2 3 4 5 6 7

Binary	Octal	Hex	Decimal
000	0	0x0	0
001	1	0x1	1
010	2	0x2	2
011	3	0x3	3
100	4	0x4	4
101	5	0x5	5
110	6	0x6	6
111	7	0x7	7

Our fringe friend: base 8



Binary : 110 100 111

Decimal : 423

Octal : 647

- Octal has 8 digits:

0 1 2 3 4 5 6 7

Binary	Octal	Hex	Decimal
000	0	0x0	0
001	1	0x1	1
010	2	0x2	2
011	3	0x3	3
100	4	0x4	4
101	5	0x5	5
110	6	0x6	6
111	7	0x7	7

Our fringe friend: base 8



8

- Ancient 18-bit computers
- Some natural languages count using spaces between fingers
- Used in **chmod** unix command



	User			Group			All		
	-	w	x	r	-	x	-	-	x
	$0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0$			$1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0$			$0 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0$		
0	3			5			1		

`chmod 0351` \leftrightarrow `chmod u=wx,g=rx,o=x`

Different bases in C

```
void main(void)
{
    int a = 10;
    int b = 010;
    int c = 0x10;

    printf("a = %d\n", a);
    printf("b = %d\n", b);
    printf("c = %d\n", c);
}
```

Different bases in C

```
void main(void)
{
    int a = 10;
    int b = 010;
    int c = 0x10;

    printf("a = %d\n", a);
    printf("b = %d\n", b);
    printf("c = %d\n", c);
}
```

```
a = 10
b = 8
c = 16
```

Summary

- Embedded systems
 - **Specialized** computing devices
 - **Limited**: I/O, memory, power, cost
 - May be **mission critical, real-time** systems
- Number systems
 - Base 2 (binary), 8 (octal), 10 (decimal), 16 (hex)
 - Conversion using **simple math**
 - Add, subtract, division with remainder, powers
 - Conversion using a **lookup table**