

$$\lim_{x \rightarrow c} f(x) = L \quad \lim_{x \rightarrow c} g(x) = M \quad L \text{ and } M \text{ are both real}$$

$$1. \lim_{x \rightarrow c} k = k$$

$$2. \lim_{x \rightarrow c} x = c$$

$$3. \lim_{x \rightarrow c} [f(x) + g(x)] = \lim_{x \rightarrow c} f(x) + \lim_{x \rightarrow c} g(x) = L + M$$

$$4. \lim_{x \rightarrow c} [f(x) - g(x)] = \lim_{x \rightarrow c} f(x) - \lim_{x \rightarrow c} g(x) = L - M$$

$$5. \lim_{x \rightarrow c} k \cdot f(x) = k \cdot \lim_{x \rightarrow c} f(x) = k \cdot L$$

$$6. \lim_{x \rightarrow c} [f(x) \cdot g(x)] = \lim_{x \rightarrow c} f(x) \cdot \lim_{x \rightarrow c} g(x) = L \cdot M$$

$$7. \lim_{x \rightarrow c} \frac{f(x)}{g(x)} = \frac{\lim_{x \rightarrow c} f(x)}{\lim_{x \rightarrow c} g(x)} = \frac{L}{M} \quad M \neq 0$$

$$8. \lim_{x \rightarrow c} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x \rightarrow c} f(x)} = \sqrt[n]{L} \quad L > 0 \text{ or } n \text{ is odd}$$

$$\lim_{x \rightarrow 2} (x^3 + 2x) = \lim_{x \rightarrow 2} x^3 + \lim_{x \rightarrow 2} 2x = \lim_{x \rightarrow 2} x \cdot \lim_{x \rightarrow 2} x \cdot \lim_{x \rightarrow 2} x + 2 \lim_{x \rightarrow 2} x$$

$$\lim_{x \rightarrow 2} x^3 + 2 \lim_{x \rightarrow 2} x$$

$$2^3 + 2(2) = 8 + 4 = 12$$

$$\lim_{x \rightarrow 2} f(x) = 4$$

$$\lim_{x \rightarrow 2} g(x) = 1$$

Find the limit ~~of~~

$$\lim_{x \rightarrow 2} \frac{2 - f(x)}{3 + g(x)}$$

$$\lim_{x \rightarrow 2} \frac{(2 - f(x))}{(3 + g(x))} = \frac{\lim_{x \rightarrow 2} 2 - \lim_{x \rightarrow 2} f(x)}{\lim_{x \rightarrow 2} 3 - \lim_{x \rightarrow 2} g(x)} = \frac{2 - 4}{3 - 1} = -\frac{1}{2}$$

Theorem 3

1. $\lim_{x \rightarrow c} f(x) = f(c)$ for any polynomial function

2. $\lim_{x \rightarrow c} r(x) = r(c)$ for any rational function with a non zero denominator at $x=c$

$$\lim_{x \rightarrow 2} (x^4 - x^2 + 1) = 2^4 - 2^2 + 1 = 13$$

$$\lim_{x \rightarrow 2} \sqrt[2]{x-1} = \sqrt[2]{\lim_{x \rightarrow 2} (x-1)} = \sqrt[2]{2-1} = 1$$